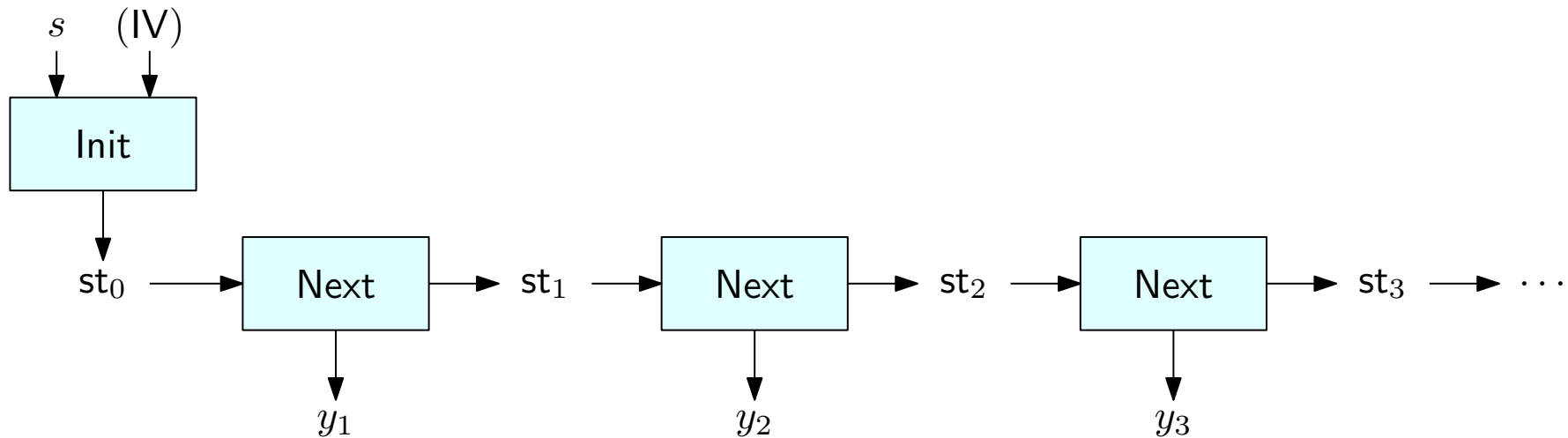


Stream ciphers (reminder)

A stream cipher is a pair of deterministic polynomial-time algorithms

- **Init:** takes a n -bit seed s , and possibly a n -bit *initialization vector* (IV), and outputs a *state* st
- **Next:** takes a state st and outputs a bit y and a new (updated) state st'

Idea: we can generate as many random bits as desired, by repeatedly calling Next



* In practice, **Next** can output multiple bits at once (e.g., a byte)

RC4

- Stands for Rivest Cipher 4
- Designed for performance in software



Ron Rivest (the R in RSA)

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- Construction does **not** use (L)FSRs
- Very simple (fits one slide!)



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WEP Encryption



Ron Rivest (the R in RSA)

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WEP Encryption

- We will see how to attack it



Ron Rivest (the R in RSA)

RC4

The state consists of:

- An array S of 256 bytes, which will always be a permutation of $\{0, \dots, 255\}$
- A pair of integers $i, j \in \{0, \dots, 255\}$

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Init(k : array of 16 bytes):

- $S \leftarrow [0, 1, 2, \dots, 255]$
- $k \leftarrow \underbrace{k \parallel k \parallel \dots \parallel k}_{16 \text{ times}}$
- $j \leftarrow 0$
- For $i \leftarrow 0, 1, \dots, 255$:
 - $j \leftarrow j + S[i] + k[i] \pmod{256}$
 - Swap $S[i]$ and $S[j]$
- Return $\langle S, i = 0, j = 0 \rangle$

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- Return the byte y and the new state $st' = \langle S, i, j \rangle$

[Demo]

Test vectors

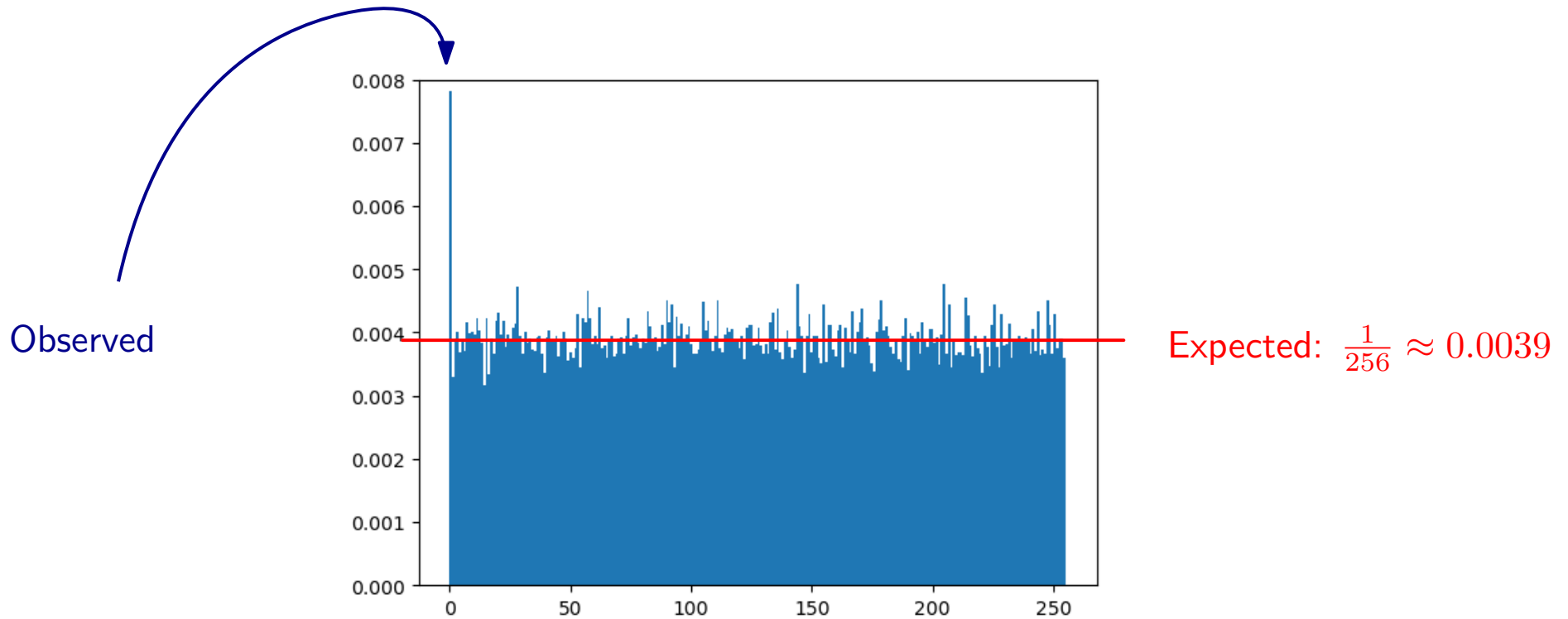
Key length: 128 bits.

key: 0x0102030405060708090a0b0c0d0e0f10

DEC	0	HEX	0:	9a c7 cc 9a	60 9d 1e f7	b2 93 28 99	cd e4 1b 97
DEC	16	HEX	10:	52 48 c4 95	90 14 12 6a	6e 8a 84 f1	1d 1a 9e 1c
DEC	240	HEX	f0:	06 59 02 e4	b6 20 f6 cc	36 c8 58 9f	66 43 2f 2b
DEC	256	HEX	100:	d3 9d 56 6b	c6 bc e3 01	07 68 15 15	49 f3 87 3f
DEC	496	HEX	1f0:	b6 d1 e6 c4	a5 e4 77 1c	ad 79 53 8d	f2 95 fb 11
DEC	512	HEX	200:	c6 8c 1d 5c	55 9a 97 41	23 df 1d bc	52 a4 3b 89
DEC	752	HEX	2f0:	c5 ec f8 8d	e8 97 fd 57	fe d3 01 70	1b 82 a2 59
DEC	768	HEX	300:	ec cb e1 3d	e1 fc c9 1c	11 a0 b2 6c	0b c8 fa 4d
DEC	1008	HEX	3f0:	e7 a7 25 74	f8 78 2a e2	6a ab cf 9e	bc d6 60 65
DEC	1024	HEX	400:	bd f0 32 4e	60 83 dc c6	d3 ce dd 3c	a8 c5 3c 16
DEC	1520	HEX	5f0:	b4 01 10 c4	19 0b 56 22	a9 61 16 b0	01 7e d2 97
DEC	1536	HEX	600:	ff a0 b5 14	64 7e c0 4f	63 06 b8 92	ae 66 11 81
DEC	2032	HEX	7f0:	d0 3d 1b c0	3c d3 3d 70	df f9 fa 5d	71 96 3e bd
DEC	2048	HEX	800:	8a 44 12 64	11 ea a7 8b	d5 1e 8d 87	a8 87 9b f5
DEC	3056	HEX	bf0:	fa be b7 60	28 ad e2 d0	e4 87 22 e4	6c 46 15 a3
DEC	3072	HEX	c00:	c0 5d 88 ab	d5 03 57 f9	35 a6 3c 59	ee 53 76 23
DEC	4080	HEX	ff0:	ff 38 26 5c	16 42 c1 ab	e8 d3 c2 fe	5e 57 2b f8
DEC	4096	HEX	1000:	a3 6a 4c 30	1a e8 ac 13	61 0c cb c1	22 56 ca cc

Output bias

Empirical distribution of the value of the 2nd output byte over 50000 samples (with keys chosen u.a.r.)

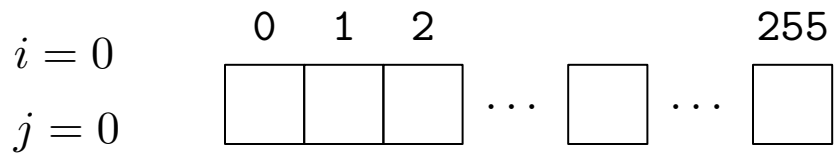


There is a bias towards 0 in the second byte output by RC4

(about twice as likely to be 0)

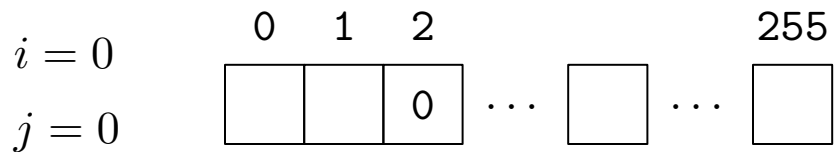
Output bias: analysis

- Consider the state immediately after **Init**
- For simplicity, think of S as a uniform permutation over $\{0, 1, \dots, 255\}$



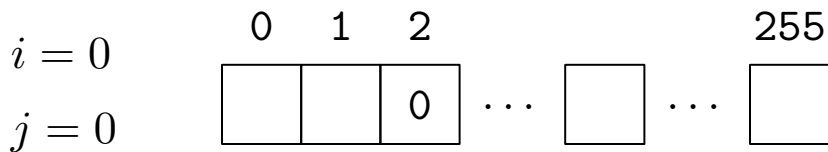
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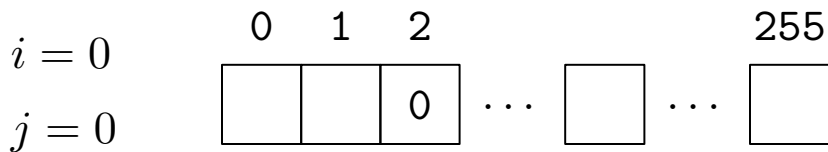
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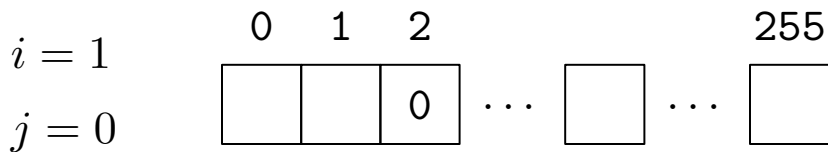
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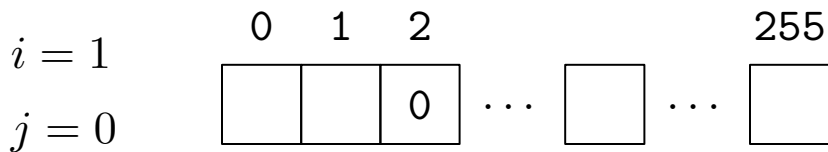
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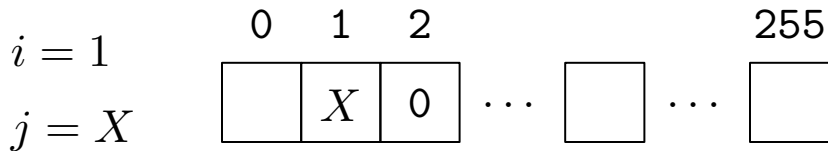


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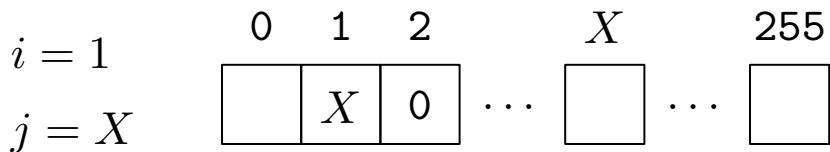
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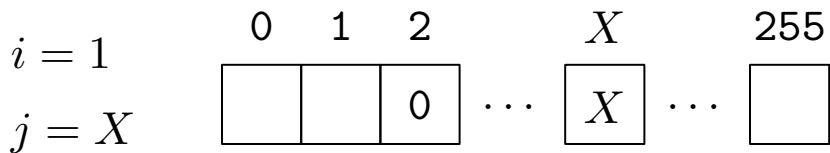
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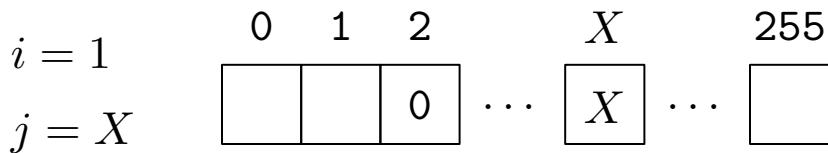


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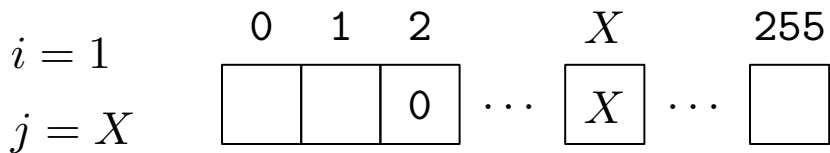


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- The rest of the code does not modify the state

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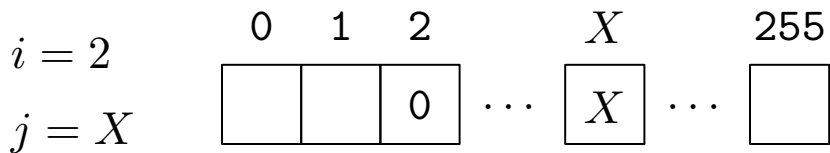


Next(st = $\langle S, i, j \rangle$): 2nd call (returns a byte)

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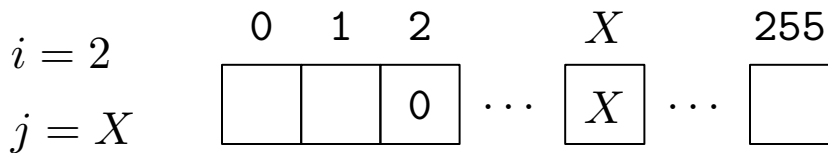


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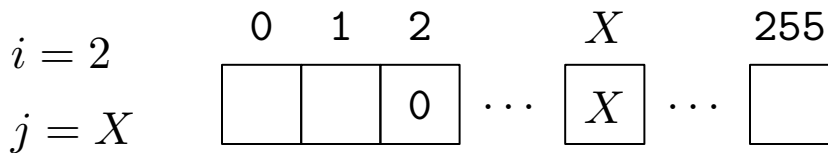


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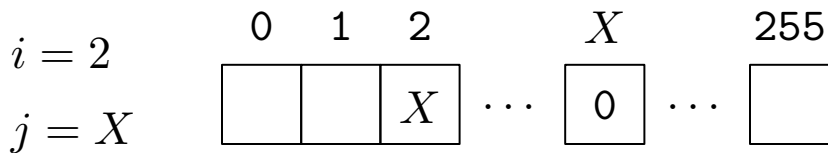


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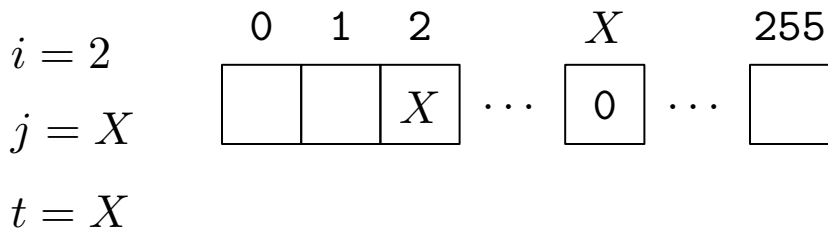


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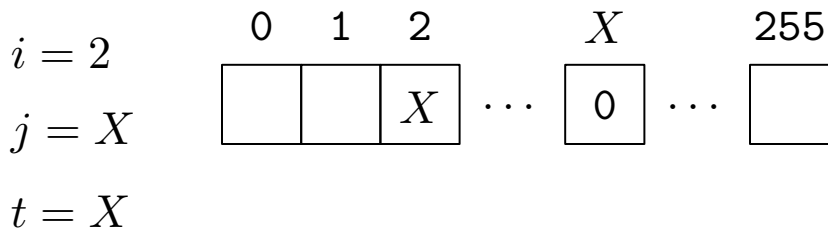


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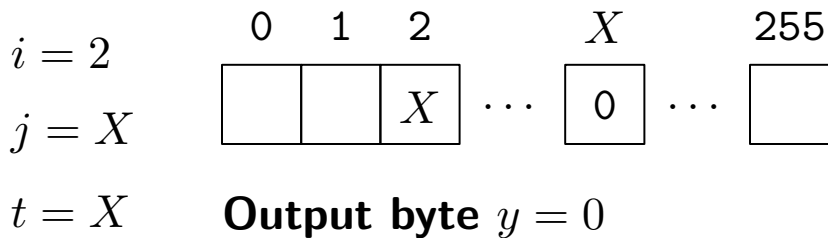


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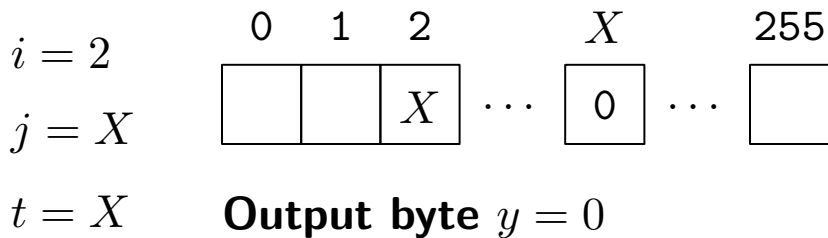


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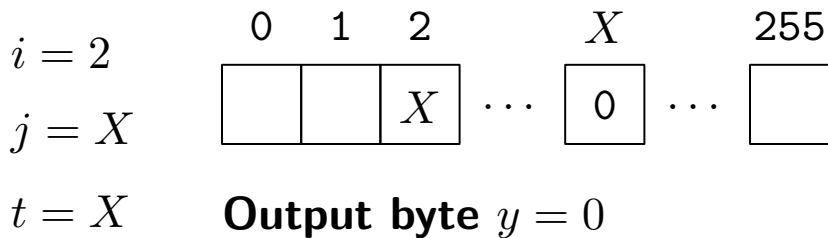
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- With probability $\approx \frac{255}{256} \approx 1$ we have that $S[2]$ is distributed “uniformly at random” after 2 iterations

Probability that the 2nd output byte is 0:

$$\approx \frac{1}{256} + 1 \cdot \frac{1}{256} = \frac{2}{256}$$

Next(st = $\langle S, i, j \rangle$):

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- The output bias is indicative of structural problems with RC4
- Other biases have been found in other bytes of the RC4 state
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- Other biases have been found in other bytes of the RC4 state
- Severe enough to allow recovery of plaintext from ciphertext when RC4 is used for encryption!

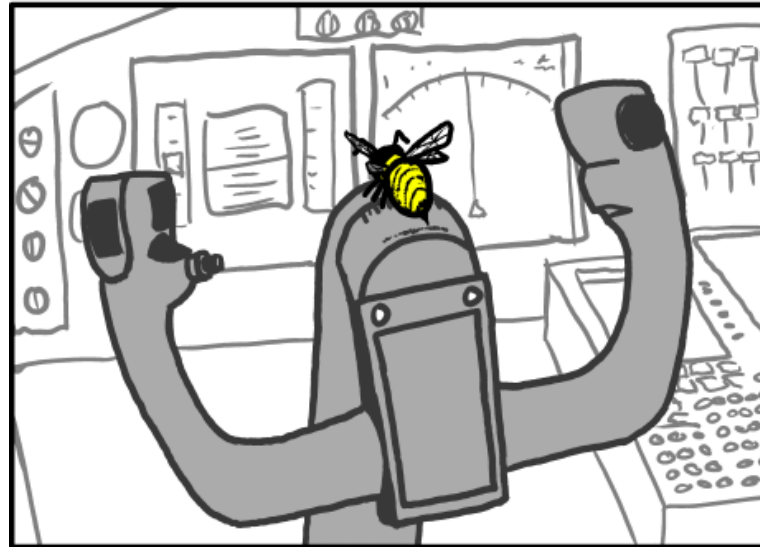


In summary: Do not use RC4!

RC4 and IVs

RC4 is **not** designed to take an IV ... but programmers don't know it and use an IV anyway

SCIENCE FACT:



PHYSICISTS STILL CAN'T EXPLAIN HOW
BUMBLEBEES CAN FLY AIRPLANES.

xkcd.com

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In practice an IV of some length ℓ (in bytes) is often used, together with a key k' of $16 - \ell$ bytes

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- We show a simplified attack that recovers the first byte of the key (i.e., $k[3]$)

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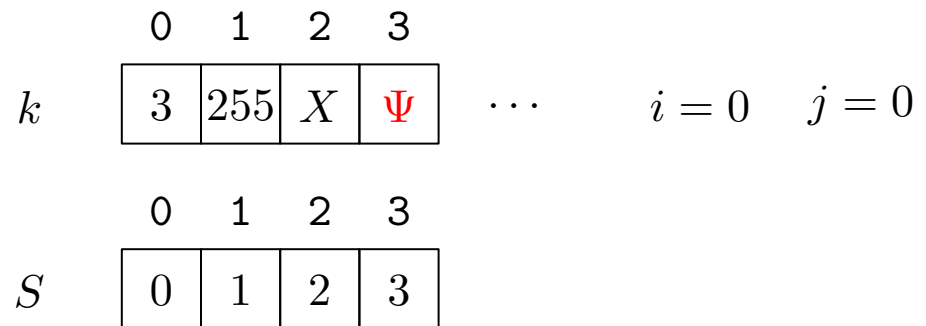
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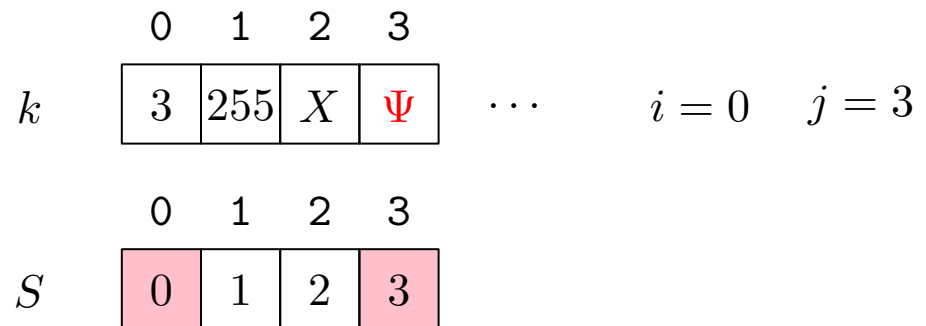
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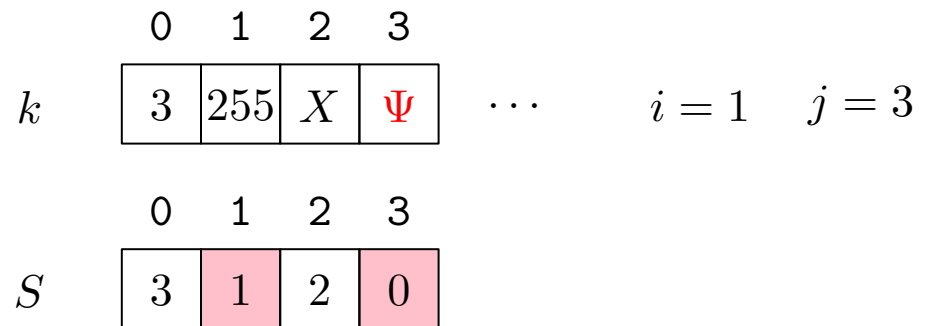
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k	3	255	X	Ψ	...	$i = 1$	$j = 3$
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S	3	1	2	0			

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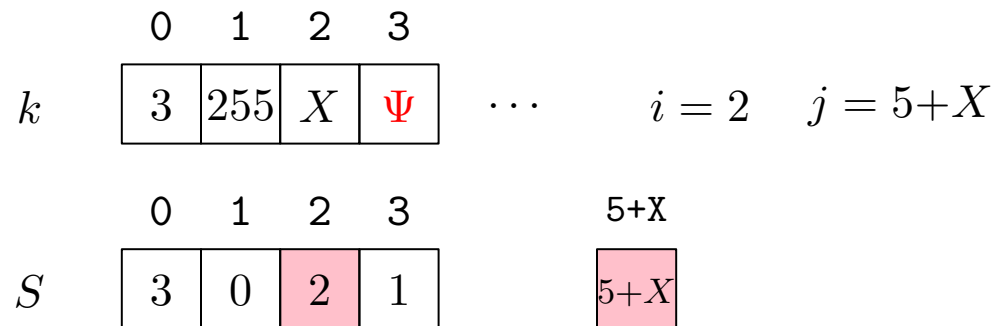
	0	1	2	3			
k	3	255	X	Ψ	...	$i = 2$	$j = 3$
	0	1	2	3			
S	3	0	2	1			

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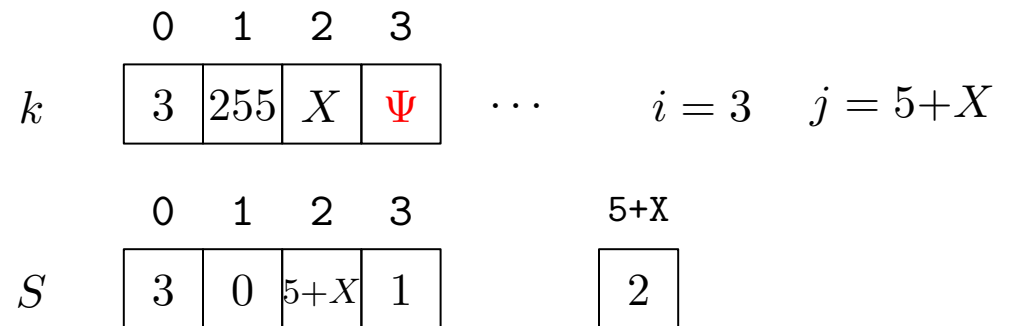
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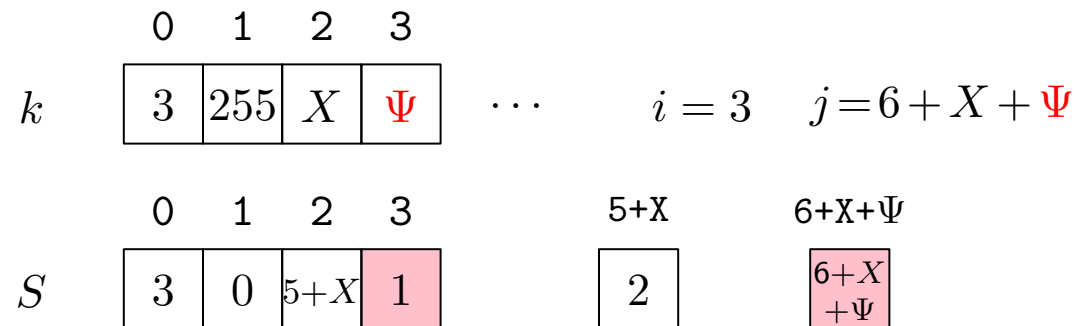
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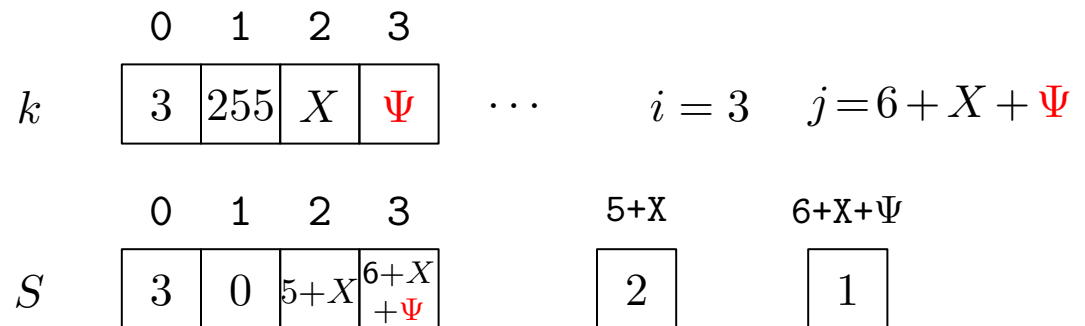
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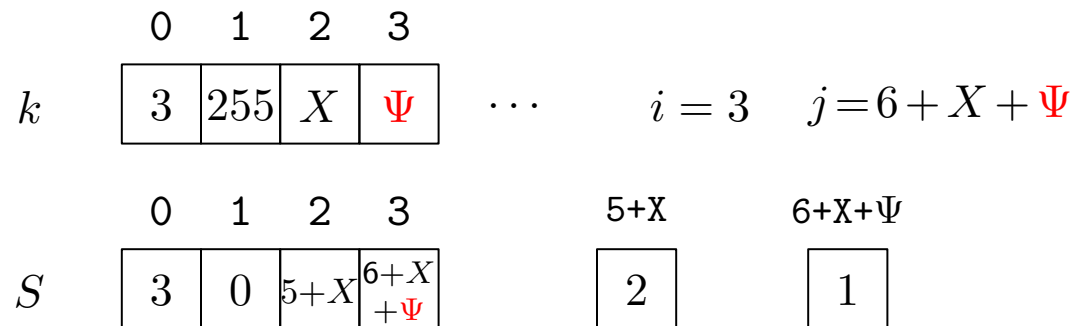
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k	$i = 1$		0	1	2	3				
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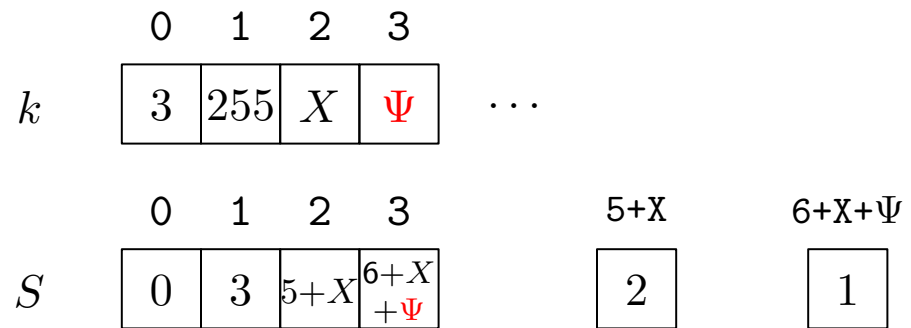
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What's the first byte output by Next (when $i = j = 0$)?

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- Repeat similar attacks to extract the next byte of the key, until the whole key is reconstructed



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- Wait for a success with some probability)

- Guess the first

- Repeat similar

```

Aircrack-ng 1.3
[00:00:00] Tested 3 keys (got 47448 IVs)
KB depth byte(vote)
0 0/ 1 DC(66304) F5(58368) F4(56576) 1F(55808) EF(55040) 28(54272)
1 0/ 1 3F(71424) 7C(59648) A2(56320) AB(56320) 11(55296) E0(55296)
2 0/ 1 73(64000) 5F(56064) 15(55552) 29(55552) 32(55040) 36(54784)
3 0/ 1 7A(67840) D1(54784) 0E(54272) 25(54272) 49(53760) 99(53760)
4 0/ 1 05(64000) B1(57600) B0(57088) 39(56576) 34(55040) 63(54272)
5 0/ 1 FE(60160) 38(57088) CC(56576) FB(55552) E4(54528) E6(54528)
6 0/ 1 6C(61696) AE(56576) 88(56320) B6(56320) 8B(55808) EE(55040)
7 0/ 1 BF(62208) D8(60672) FC(56320) 14(55808) 73(55808) 7C(55296)
8 0/ 1 68(65024) 09(56064) 31(56064) 30(55296) A0(55040) 8D(54528)
9 0/ 1 A6(60160) 72(57856) 4F(56320) 5B(56320) 7F(56064) 88(56064)
10 0/ 2 07(58112) AF(57344) 27(56320) BB(56320) 4A(55040) 42(54528)
11 0/ 1 2F(57856) E6(56832) BD(56320) B5(55040) 1F(54272) DF(54272)
12 0/ 1 DF(67072) 27(57088) 35(56832) FB(56832) 07(56576) 57(55040)

KEY FOUND! [ DC:3F:73:7A:05:FE:6C:BF:68:A6:6B:2F:DF ]
Decrypted correctly: 100%
    
```

leaked (with some

s reconstructed



ChaCha20

Introduced in 2008. Secure replacement for RC4

Takes a 256-bit key k and a 64-bit IV



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Relies on additions, rotations, and XORs of 32-bit words
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The core of ChaCha20 is a fixed permutation $P : \{0, 1\}^{512} \rightarrow \{0, 1\}^{512}$ on 512-bit strings

The permutation P is used to construct a keyed function with a 256-bit key, 128-bit inputs and 512-bit outputs

$$F_k(x) = P(\text{constant} \parallel k \parallel x) \boxplus (\text{constant} \parallel k \parallel x)$$



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\boxplus denotes word-wise modular addition (of 32-bit words)



Daniel J.
Bernstein

ChaCha20

Introduced in 2008. Secure replacement for RC4

Takes a 256-bit key k and a 64-bit IV

Relies on additions, rotations, and XORs of 32-bit words
(all of which typically require just one assembly instruction)

The core of ChaCha20 is a fixed permutation $P : \{0, 1\}^{512} \rightarrow \{0, 1\}^{512}$ on 512-bit strings

The permutation P is used to construct a keyed function with a 256-bit key, 128-bit inputs and 512-bit outputs

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Not patented. Several public domain implementations available



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Block Ciphers

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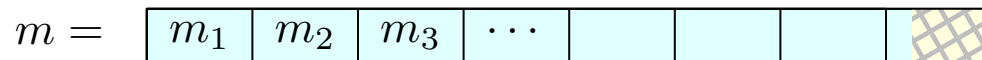
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Padding (with care)

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Recall that we can always build a stream cipher from a block cipher

For example:

Init(s, IV):

- Output $(s, IV, 0)$

Next(st):

- Unpack the state in $(s, IV, \langle i \rangle)$
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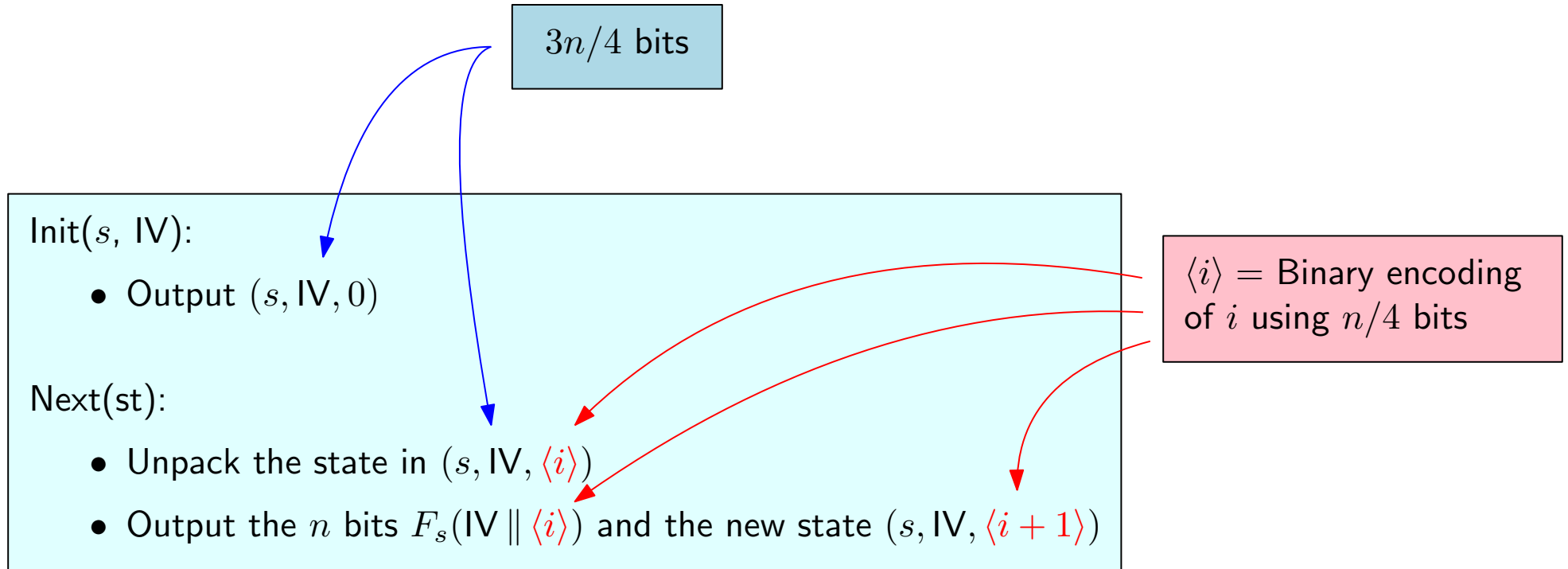
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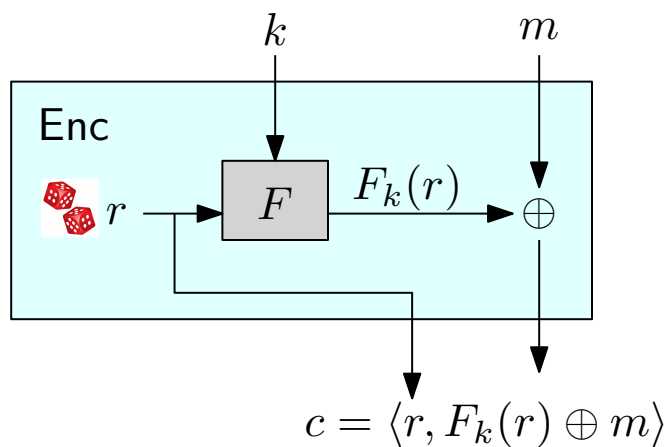
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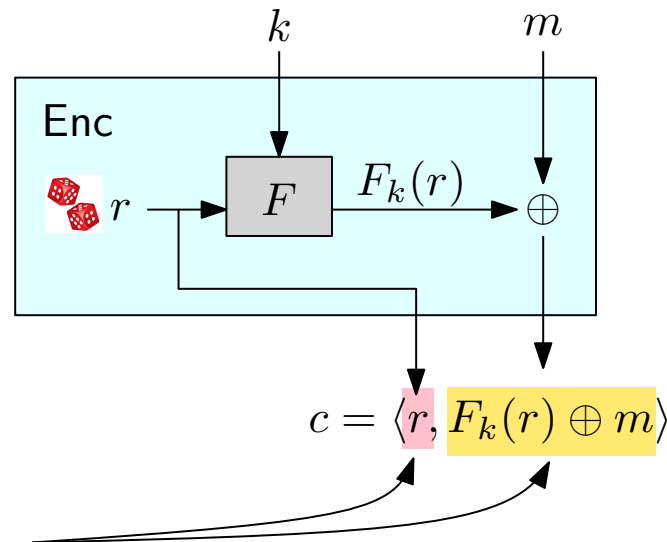
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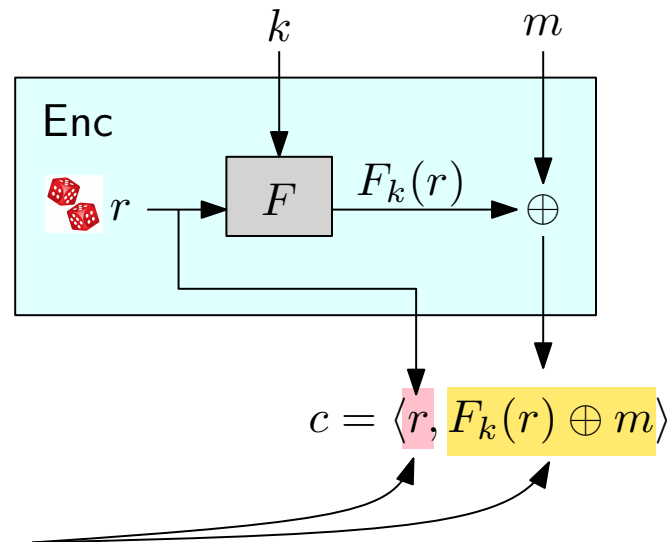


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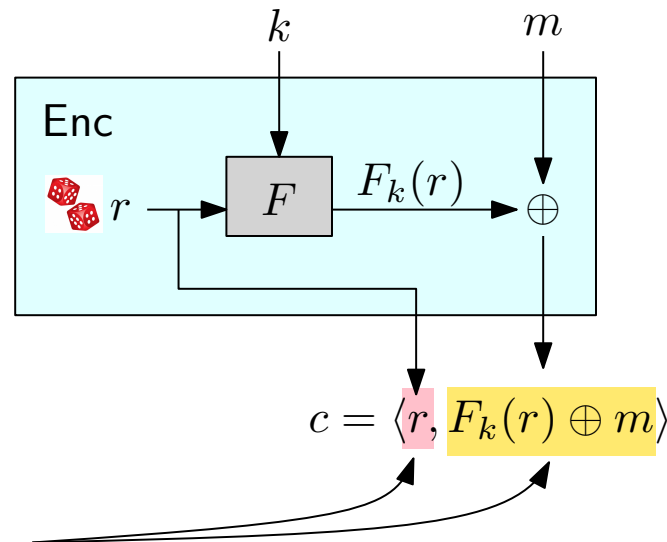


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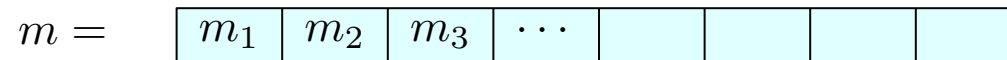
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Electronic Code Book (ECB) mode

First idea:

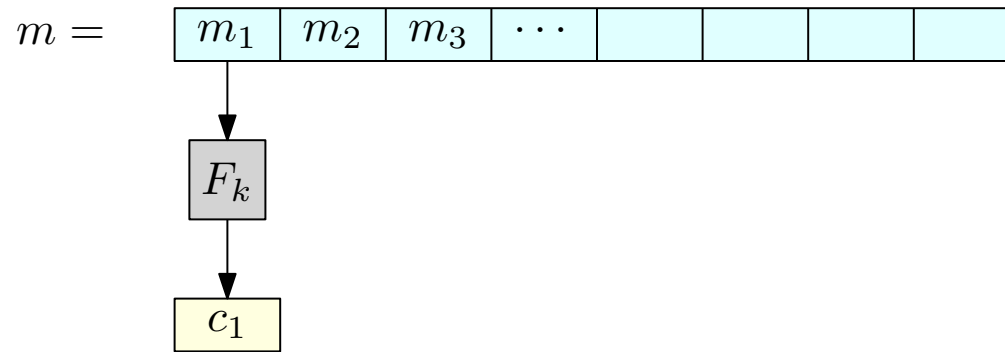
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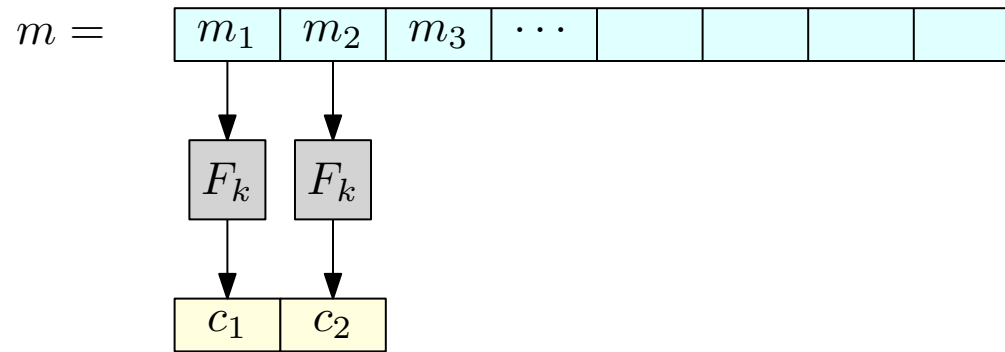
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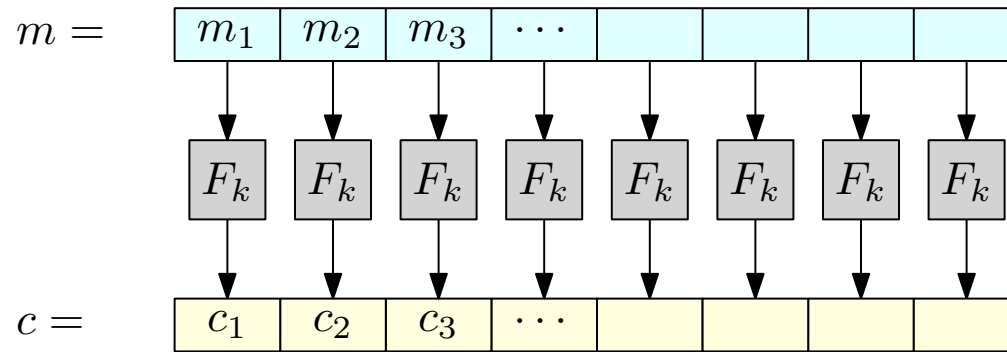
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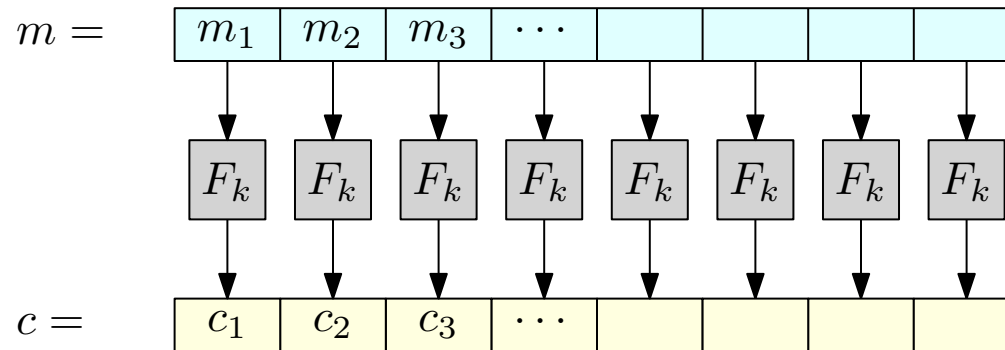
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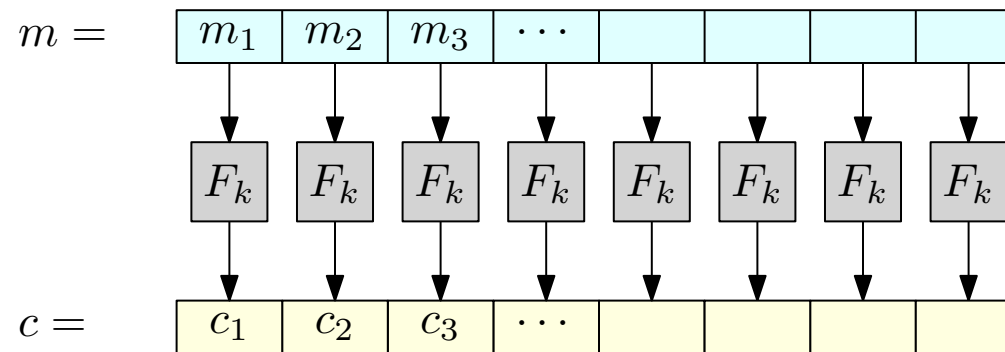
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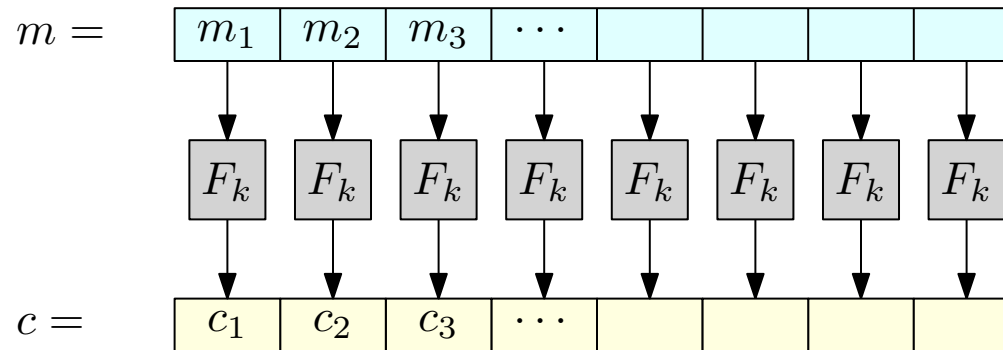
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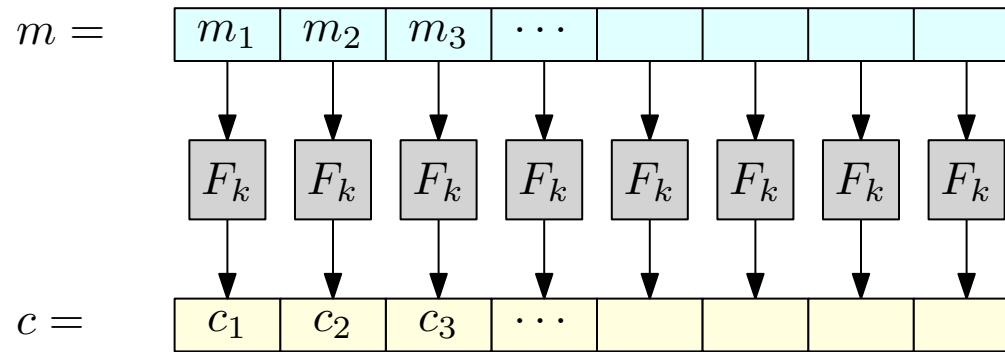
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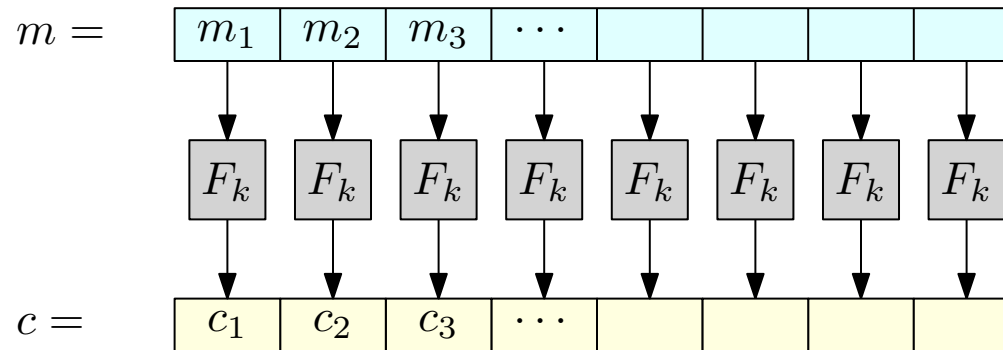
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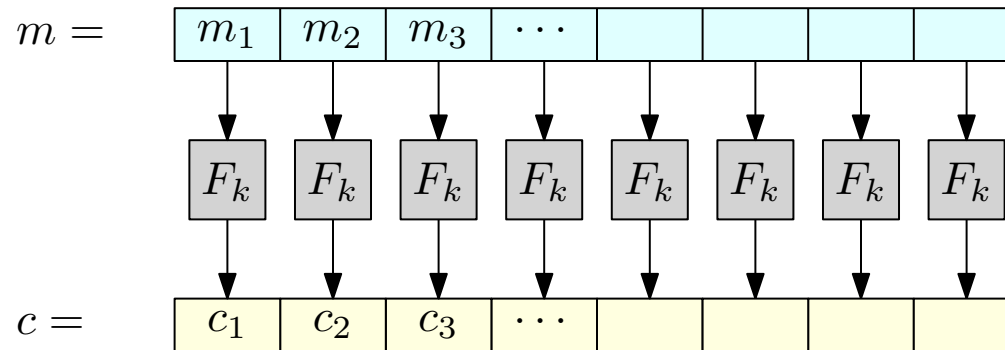
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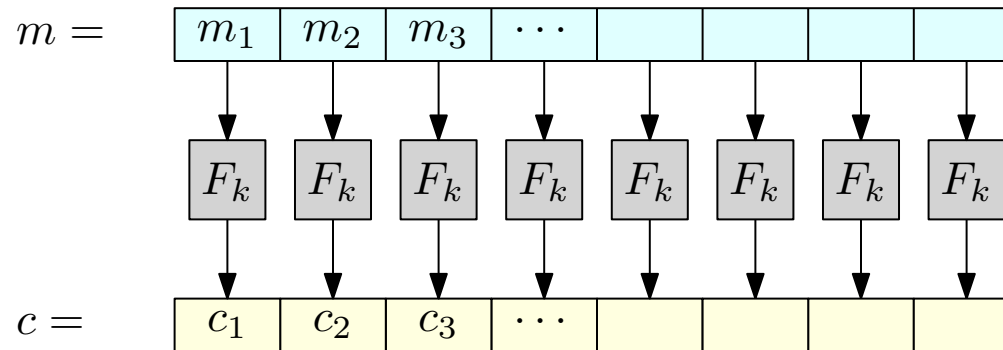
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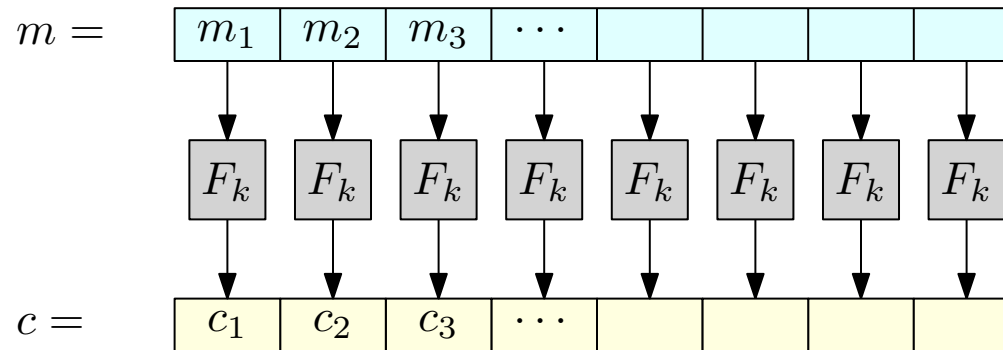
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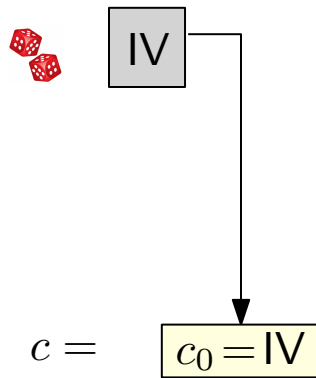
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Never use ECB!

Cipher Block Chaining (CBC) mode

$m =$

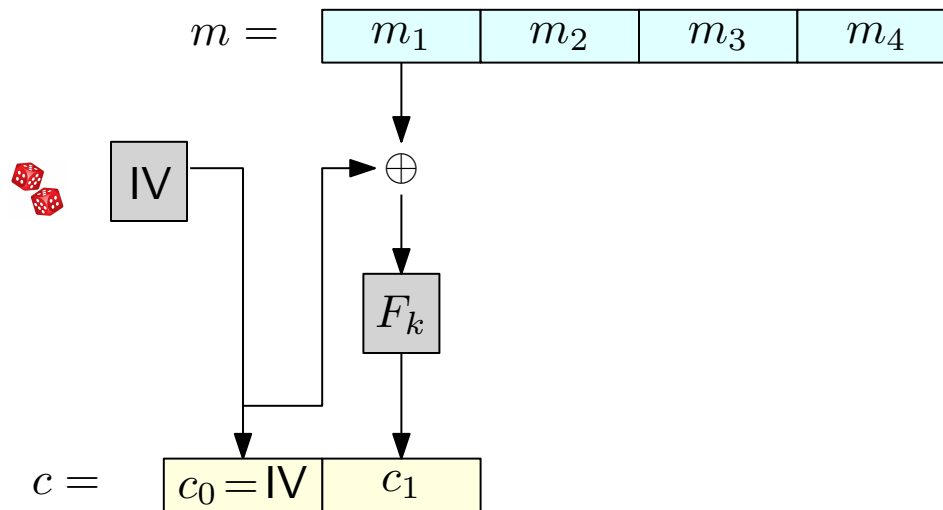
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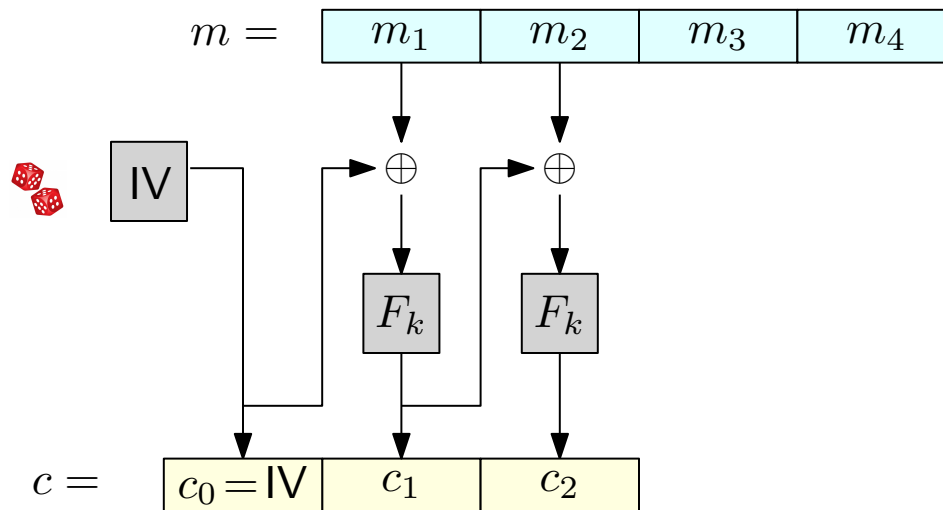


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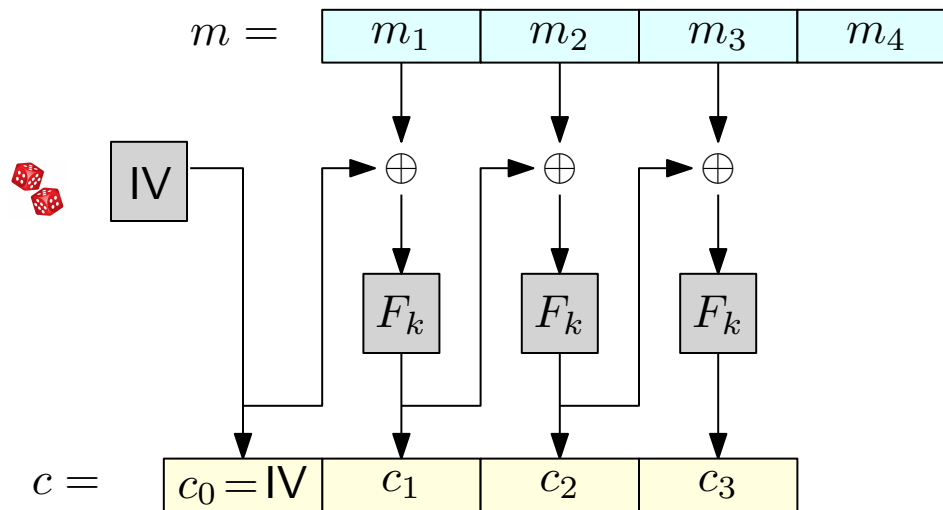


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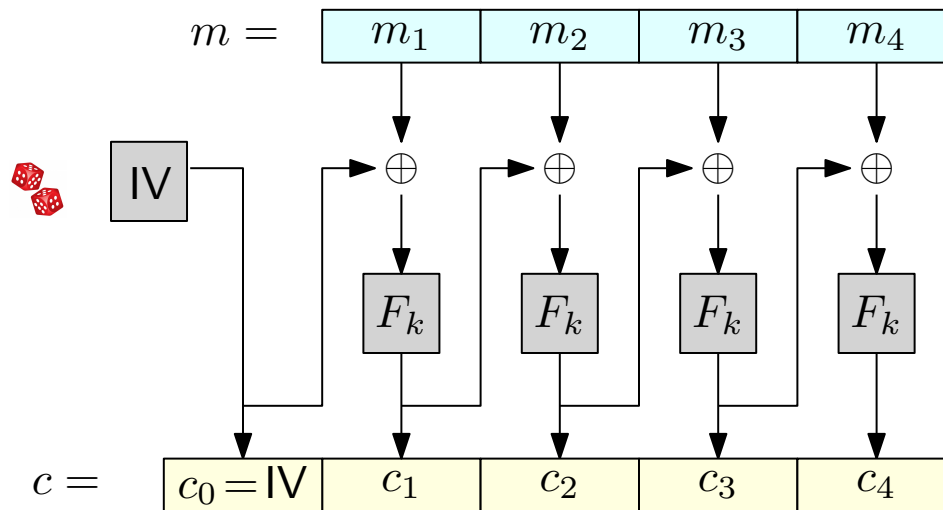


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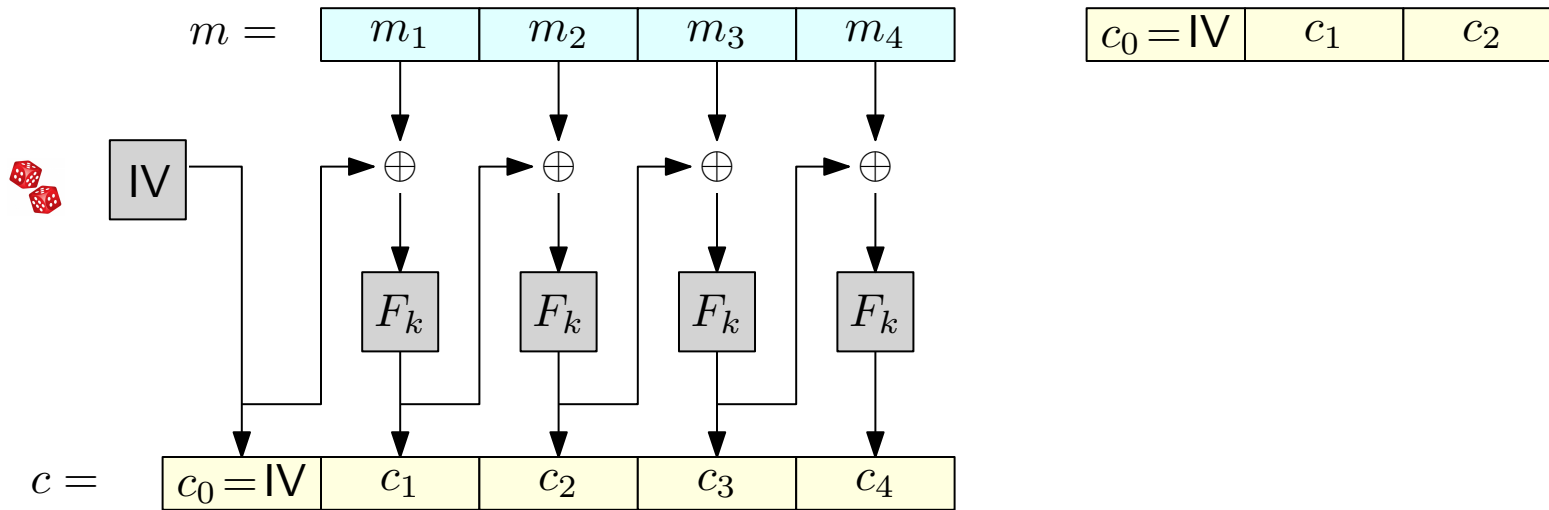


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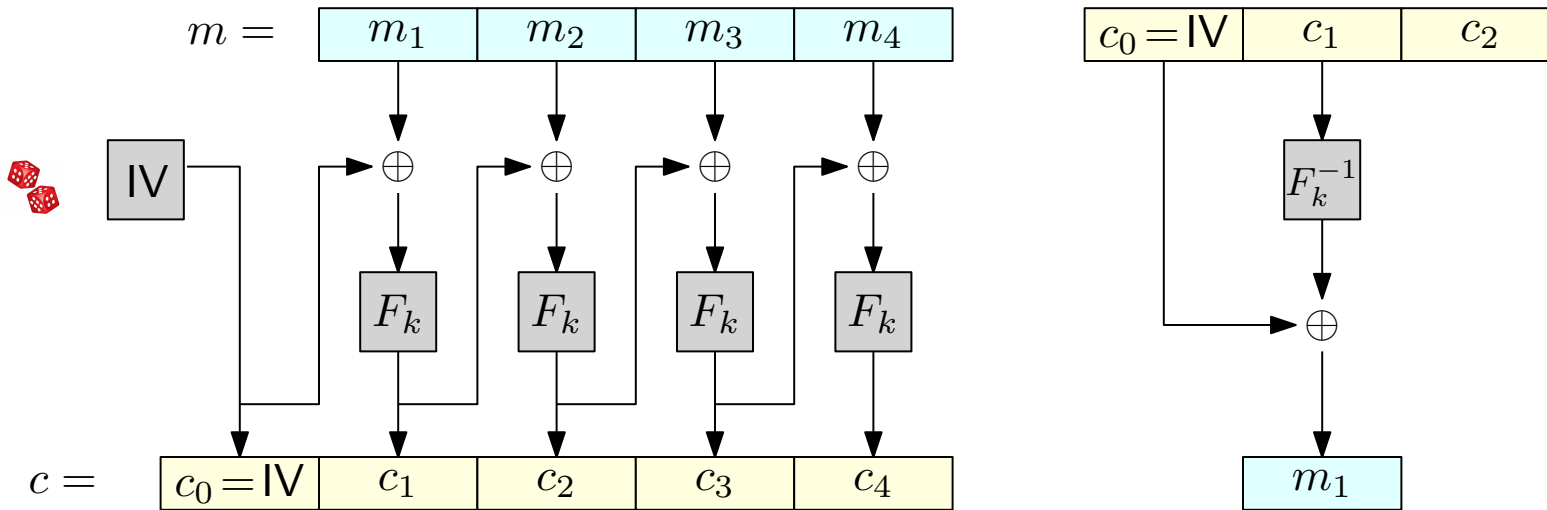
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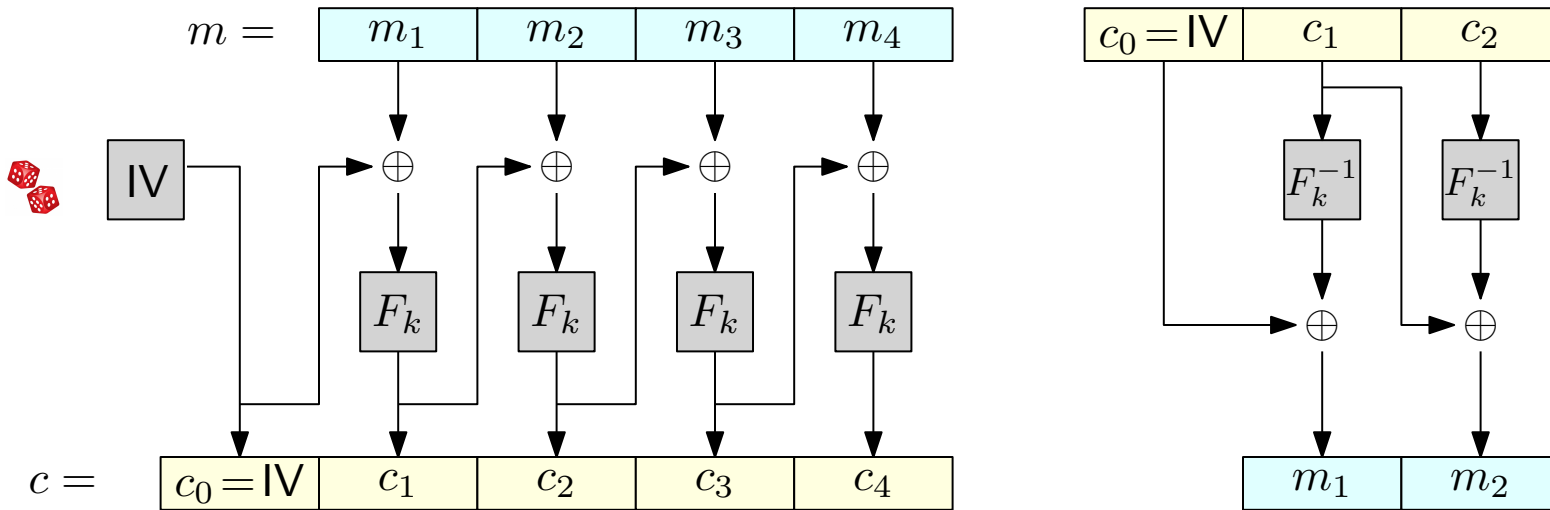
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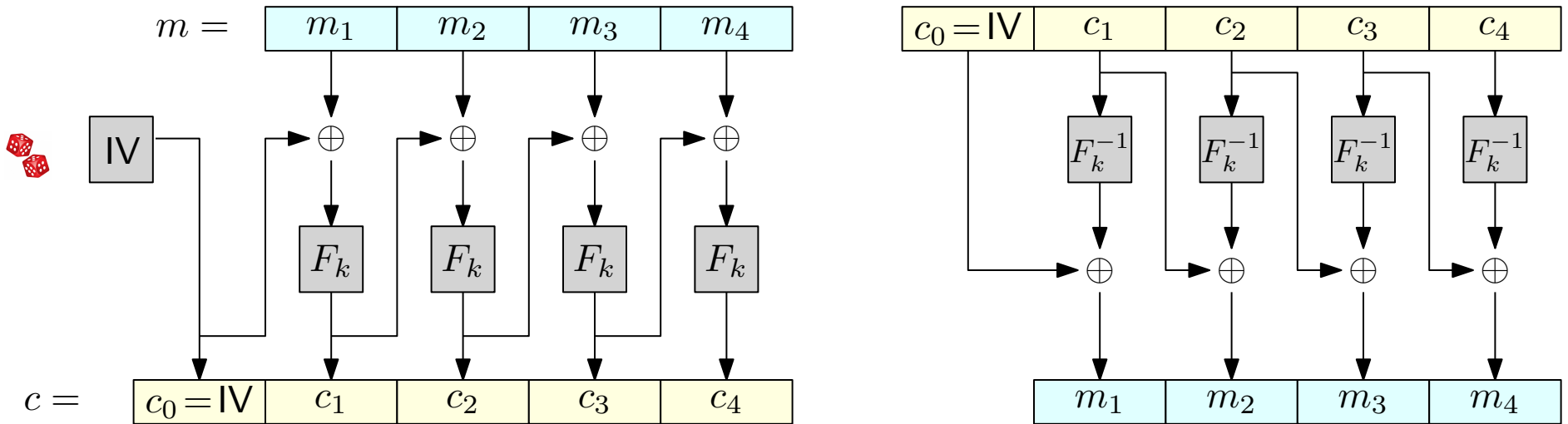
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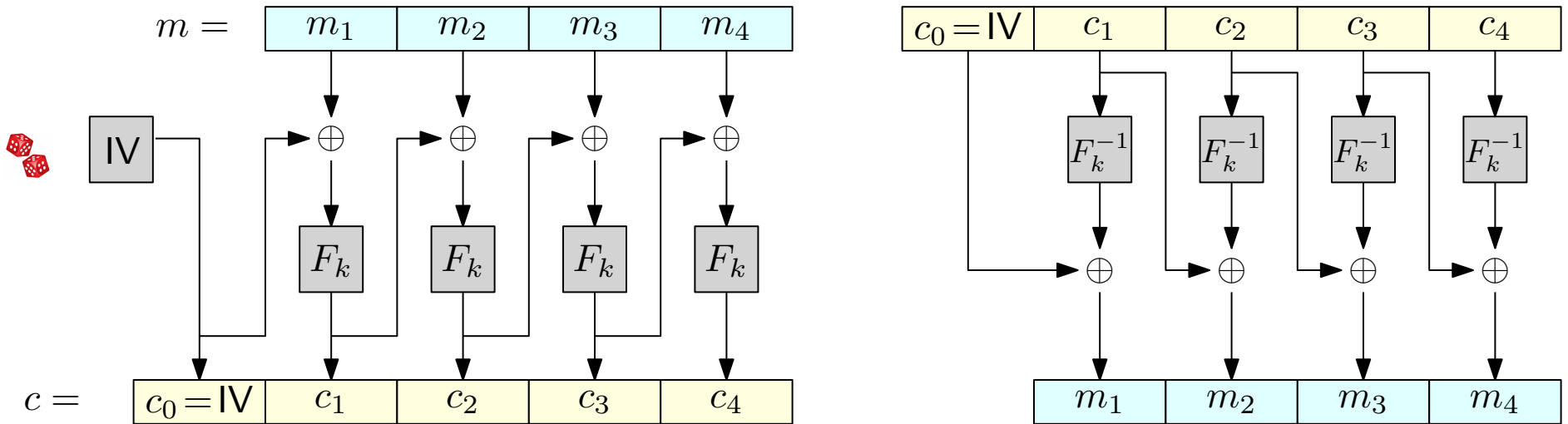
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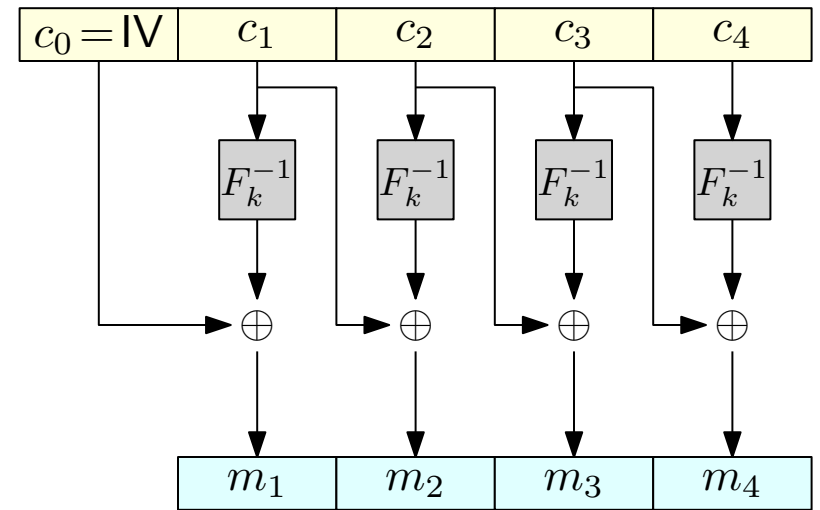
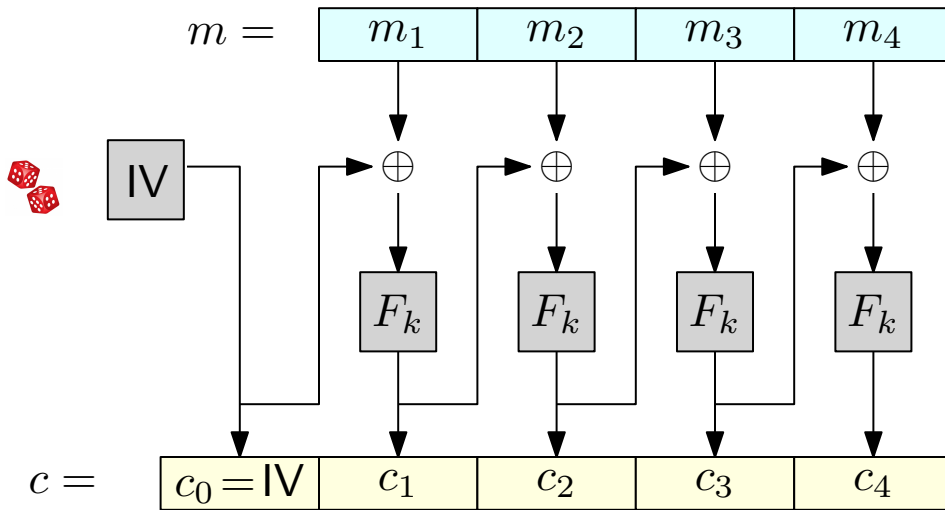


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(but decryption can be done in parallel)

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Is CBC mode CPA secure?

Cipher Block Chaining (CBC) mode

Is CBC mode CPA secure? Yes!*

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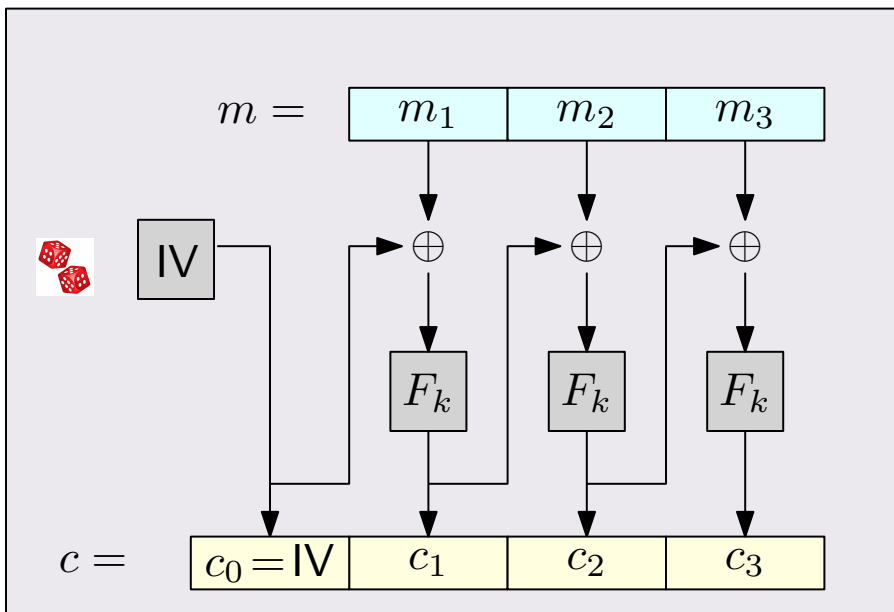


*But, depending on the implementation, it might be vulnerable to some subtle attacks (not really a fault of the encryption scheme, but something to be aware of)

Chained CBC mode

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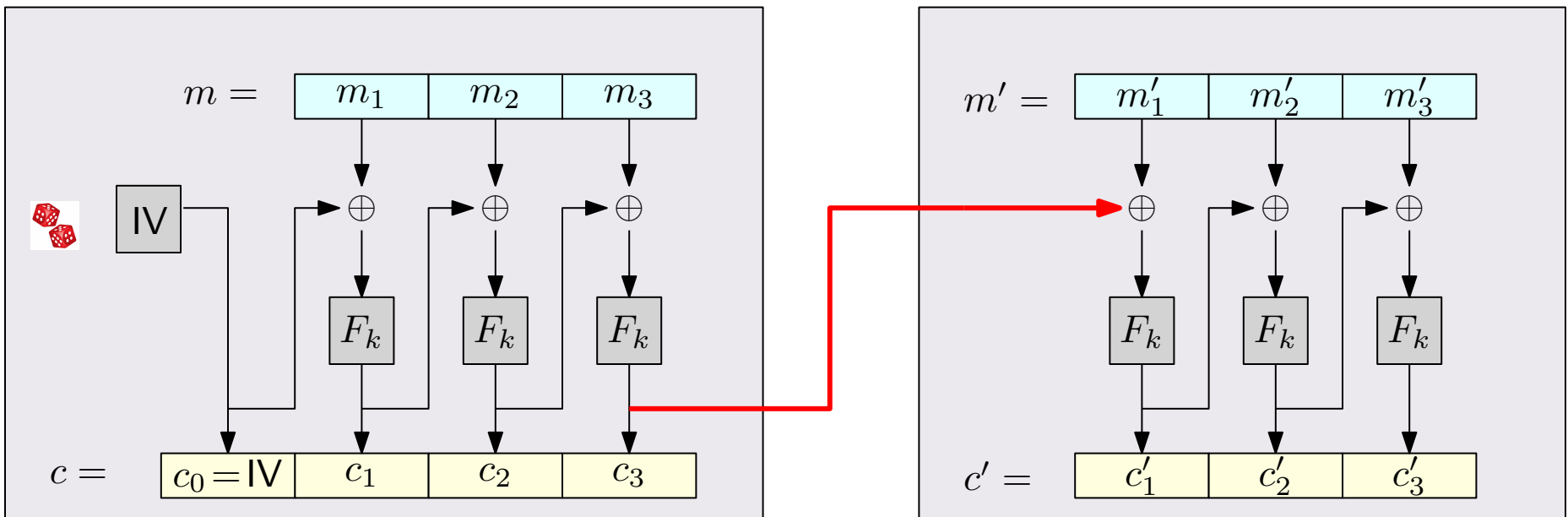
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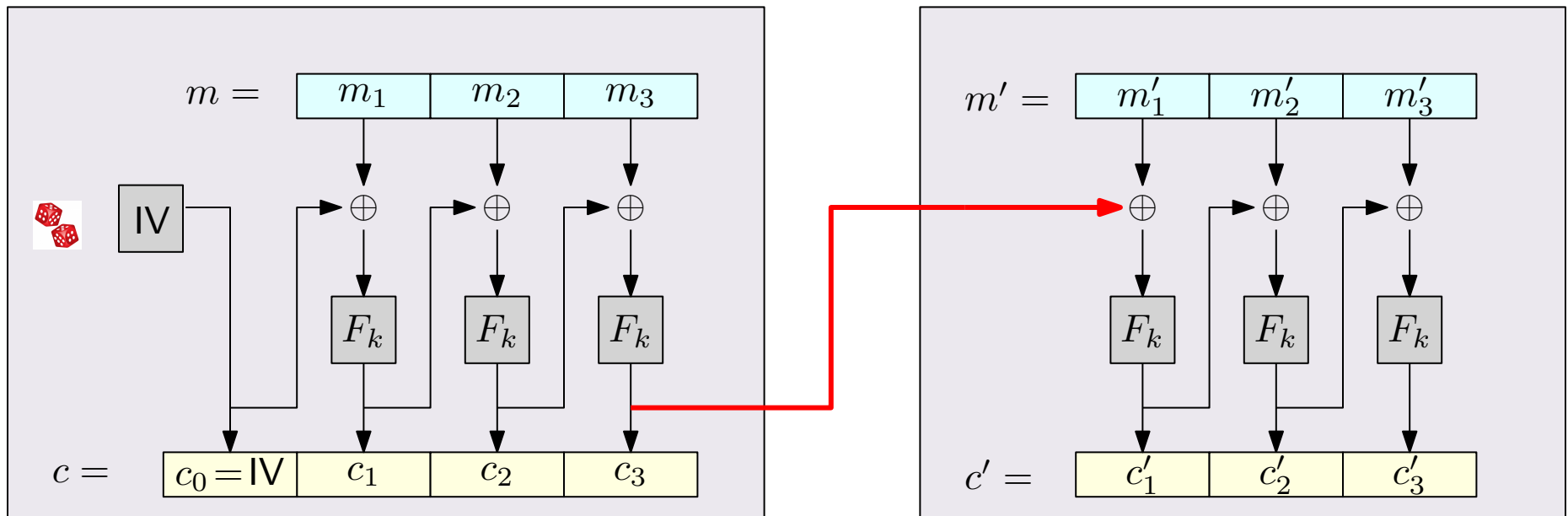
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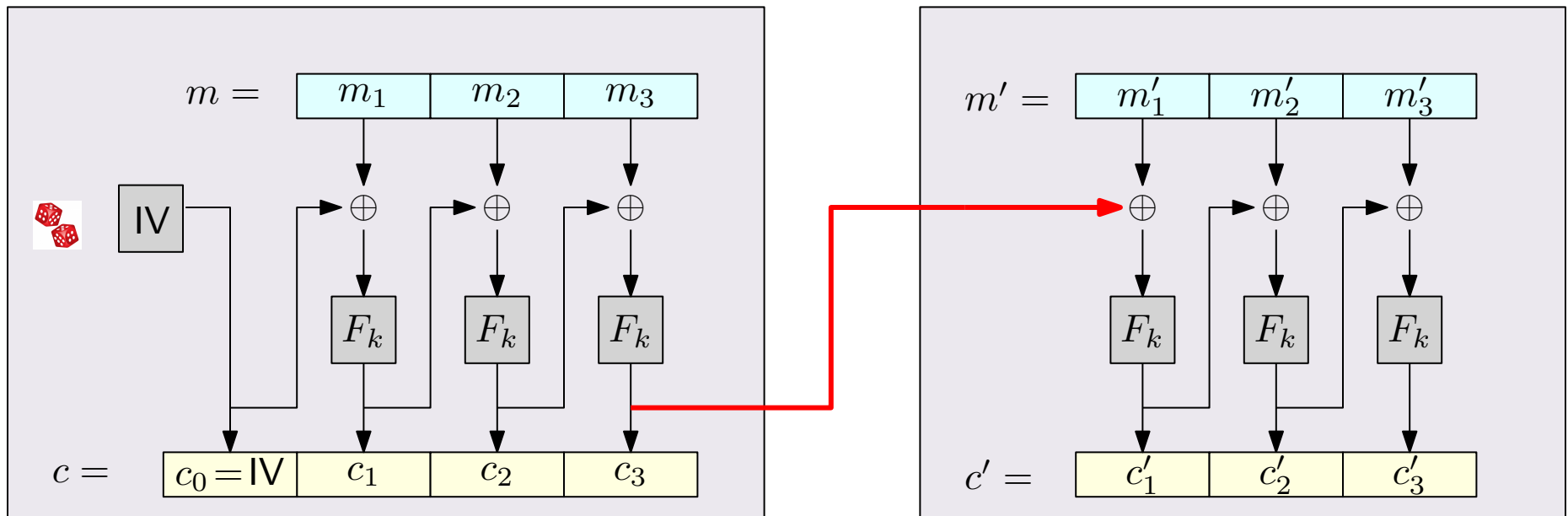


Security of Chained CBC mode



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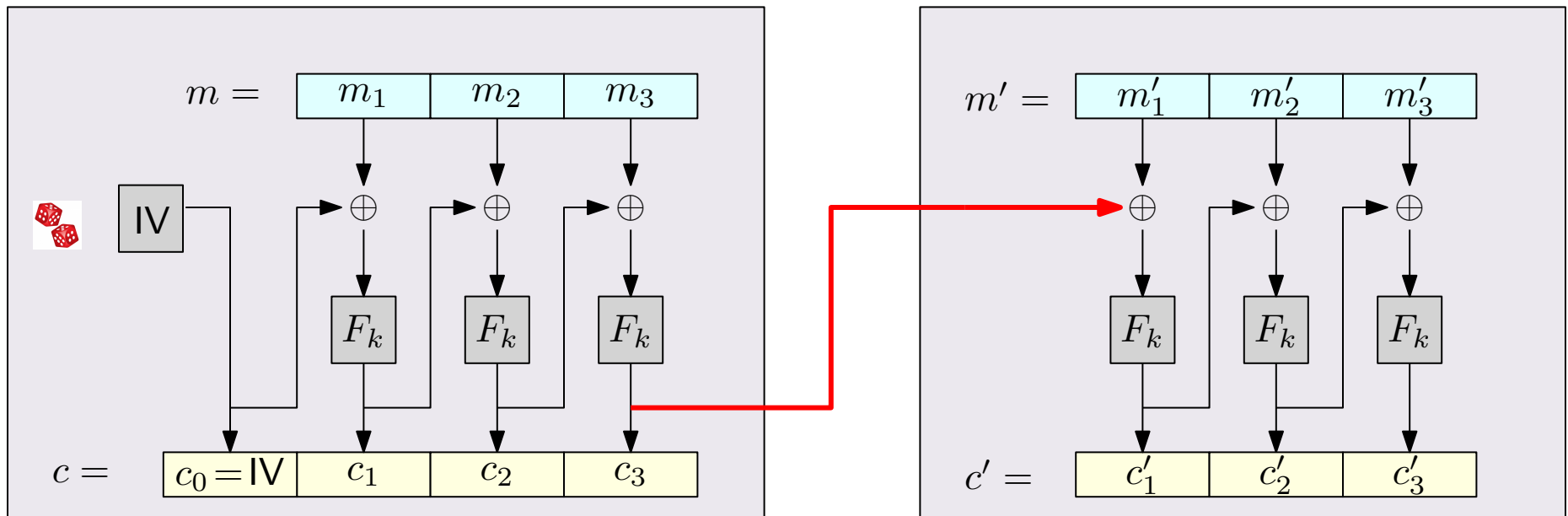
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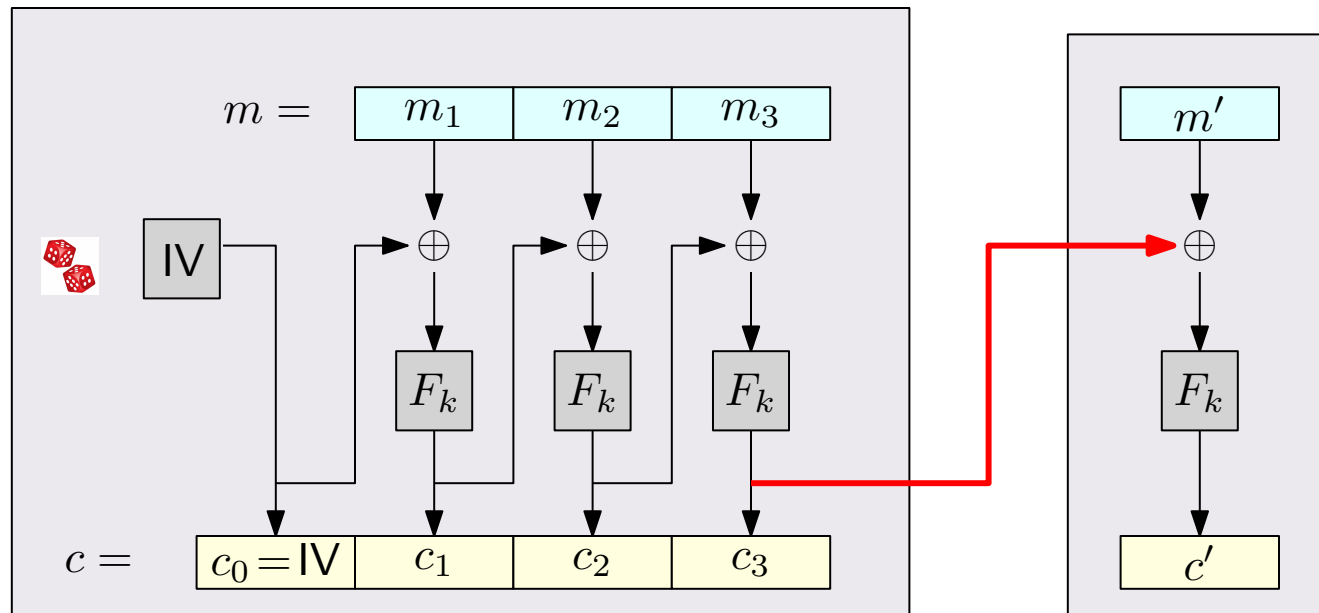


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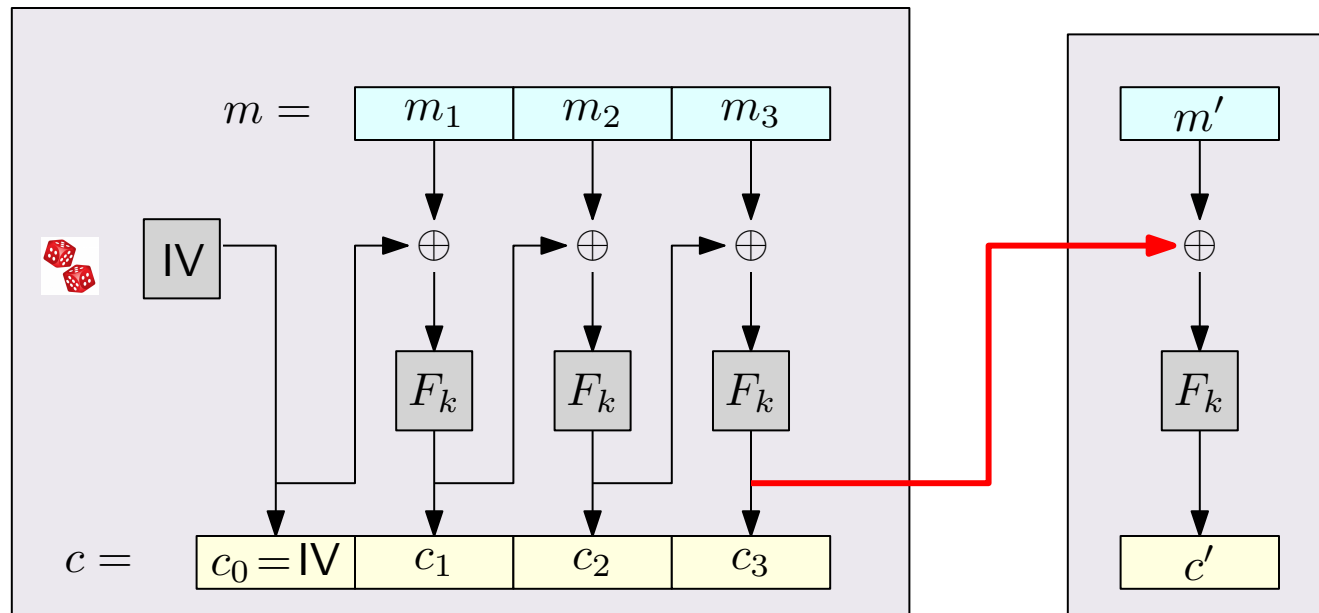
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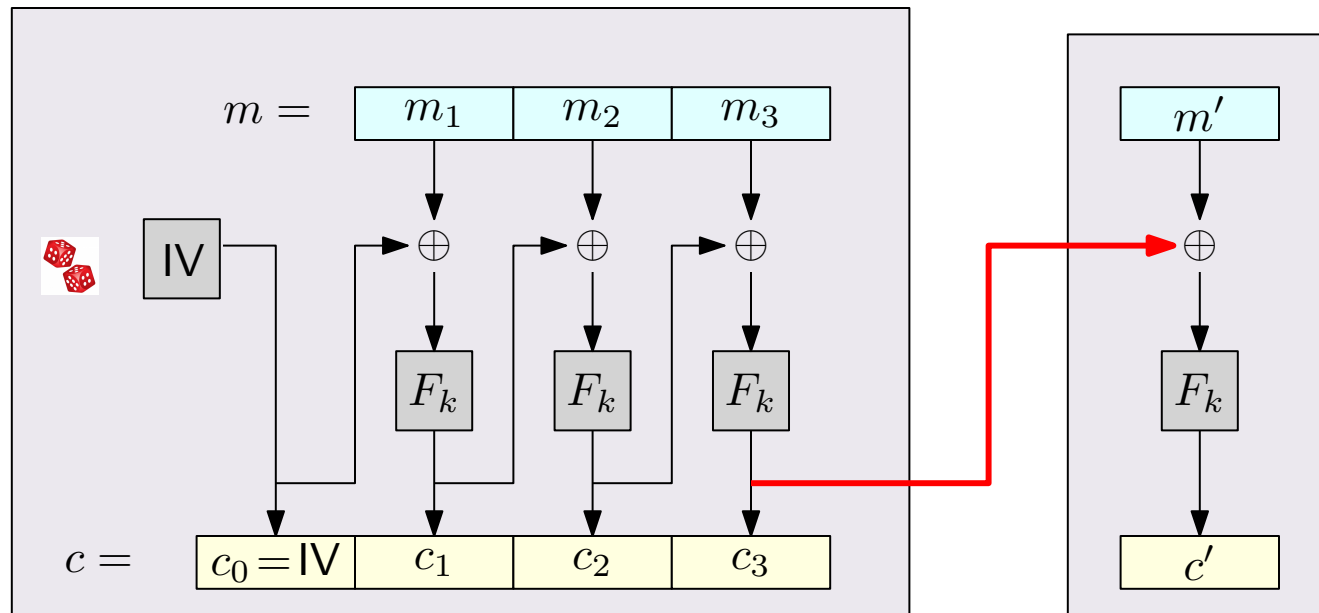
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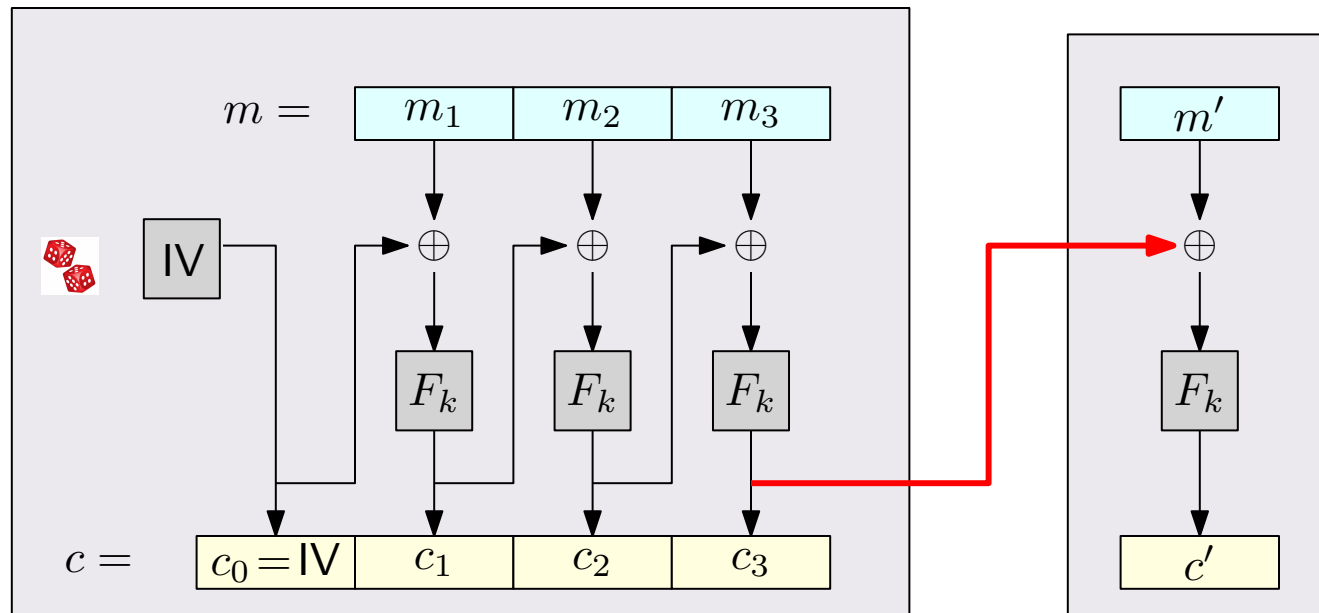


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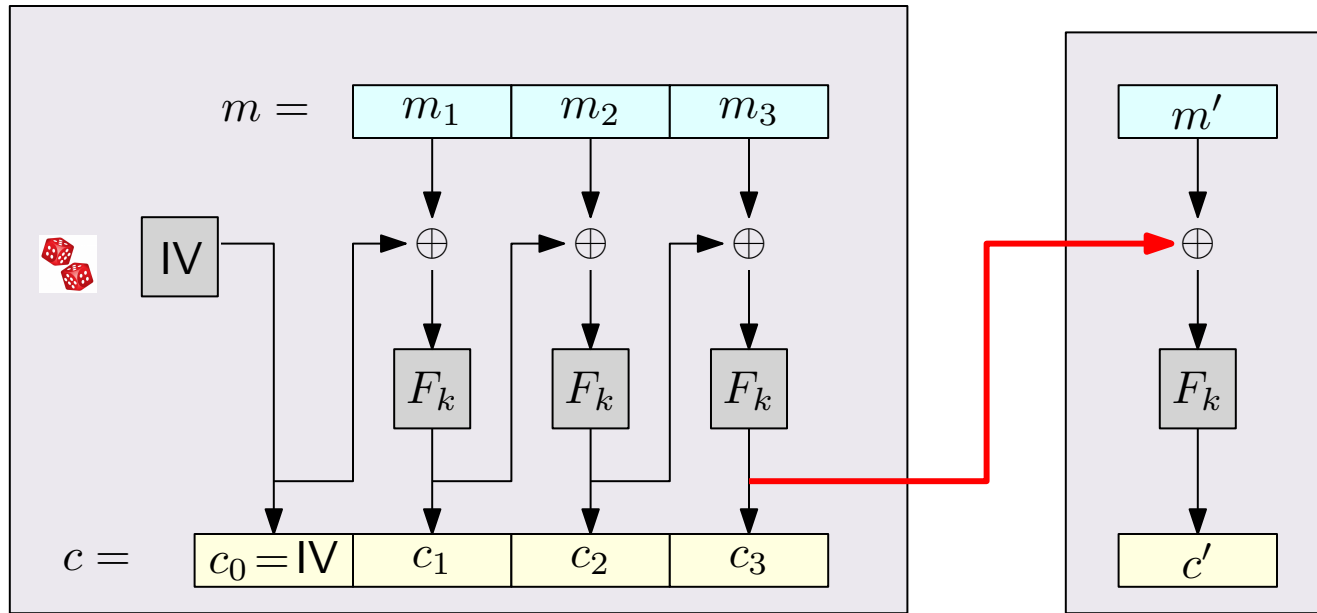


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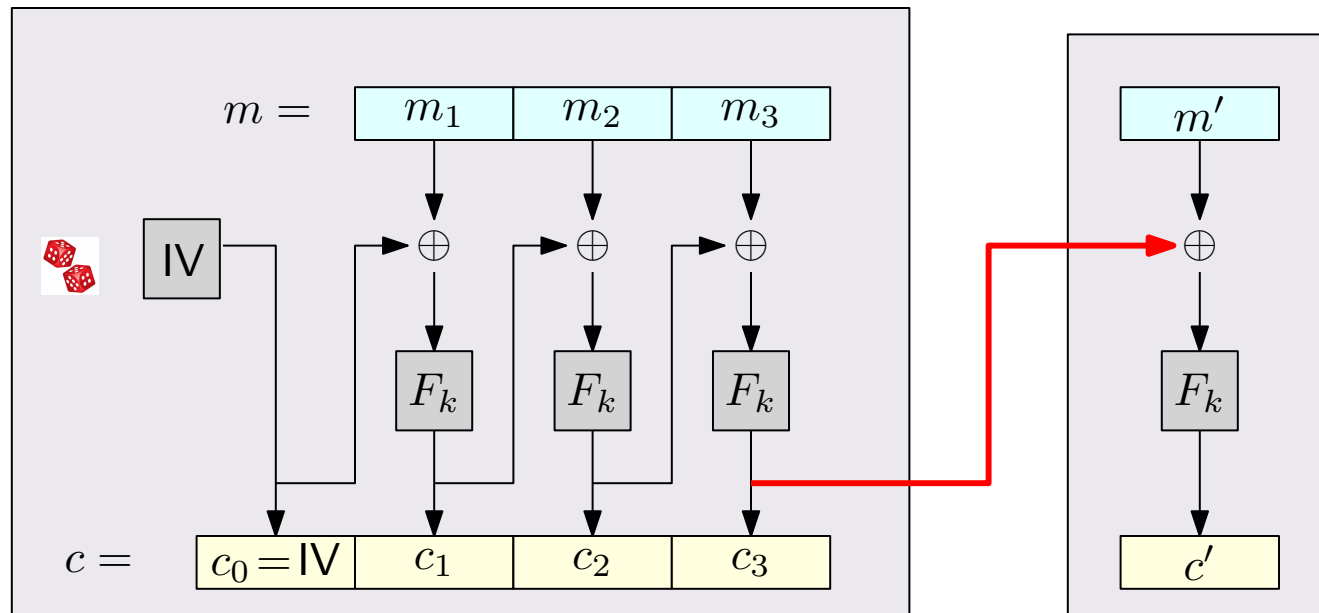


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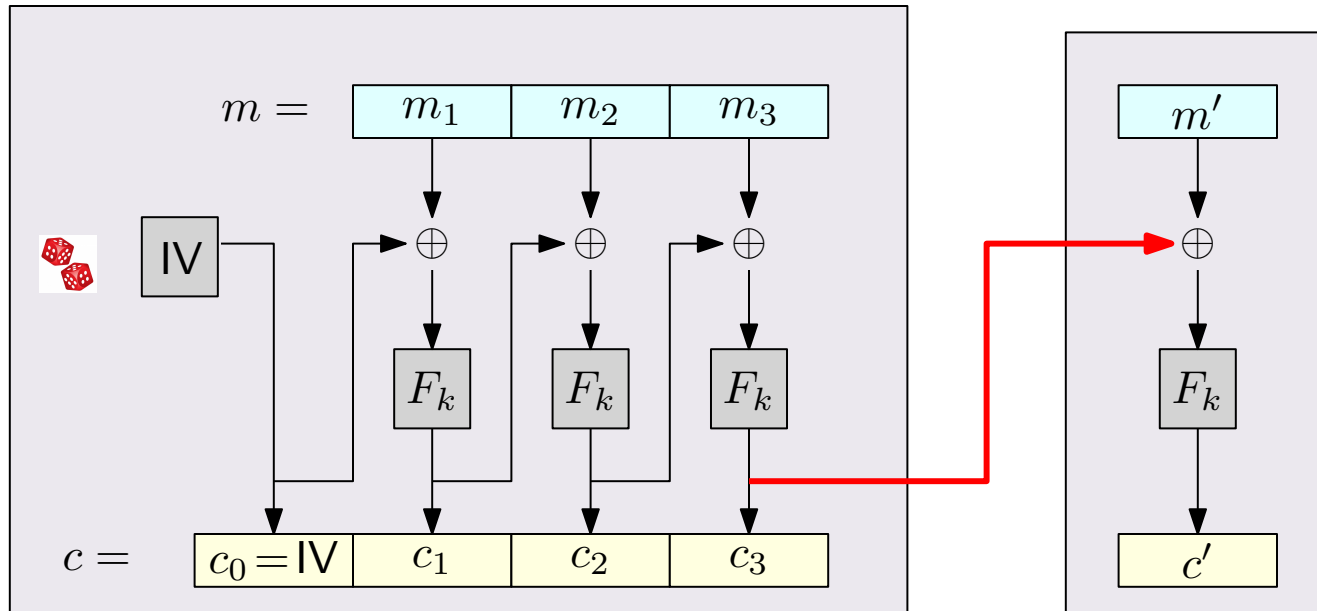


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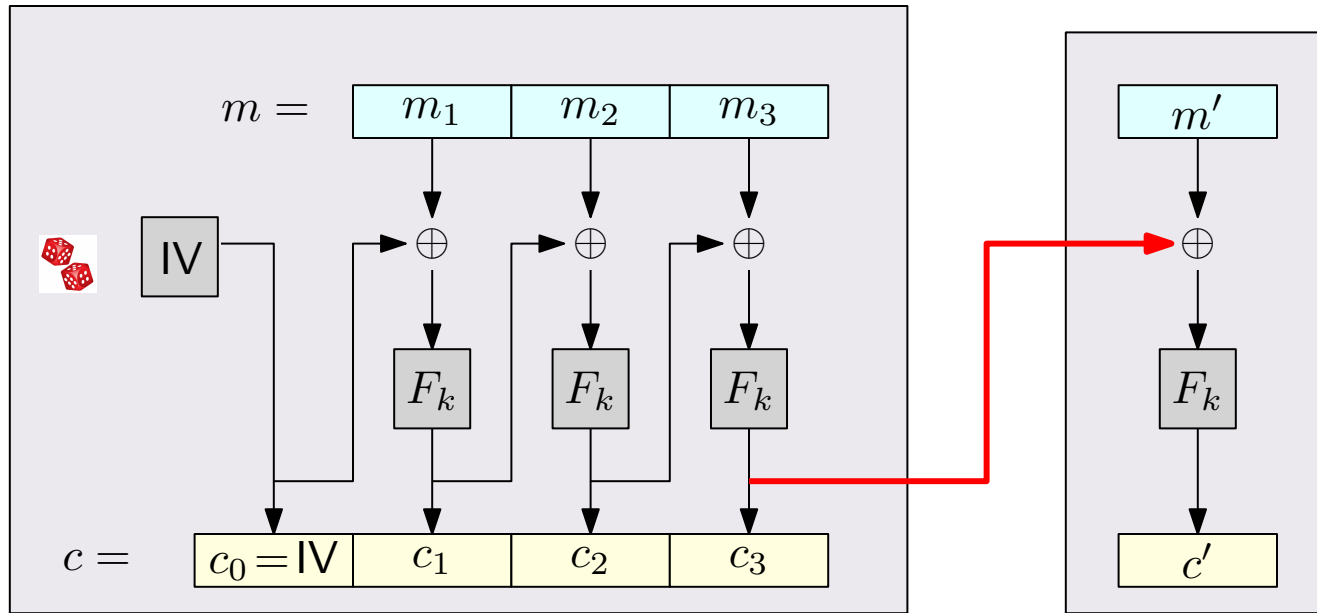
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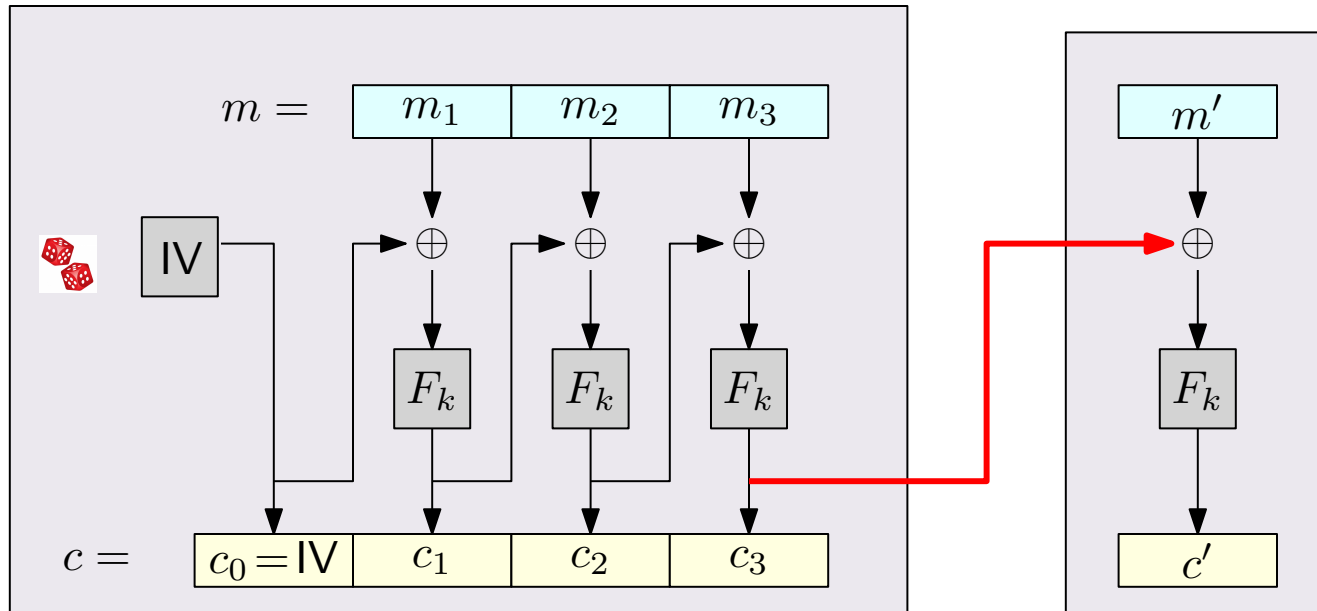
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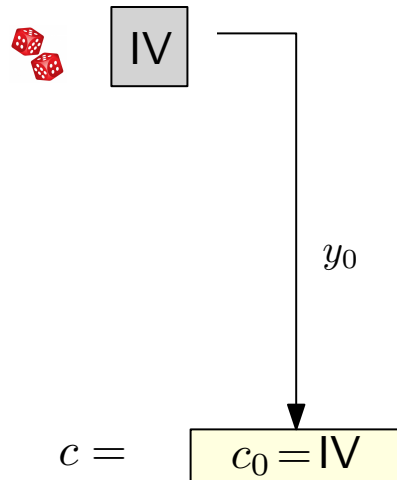
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Output Feedback (OFB) mode

$m =$

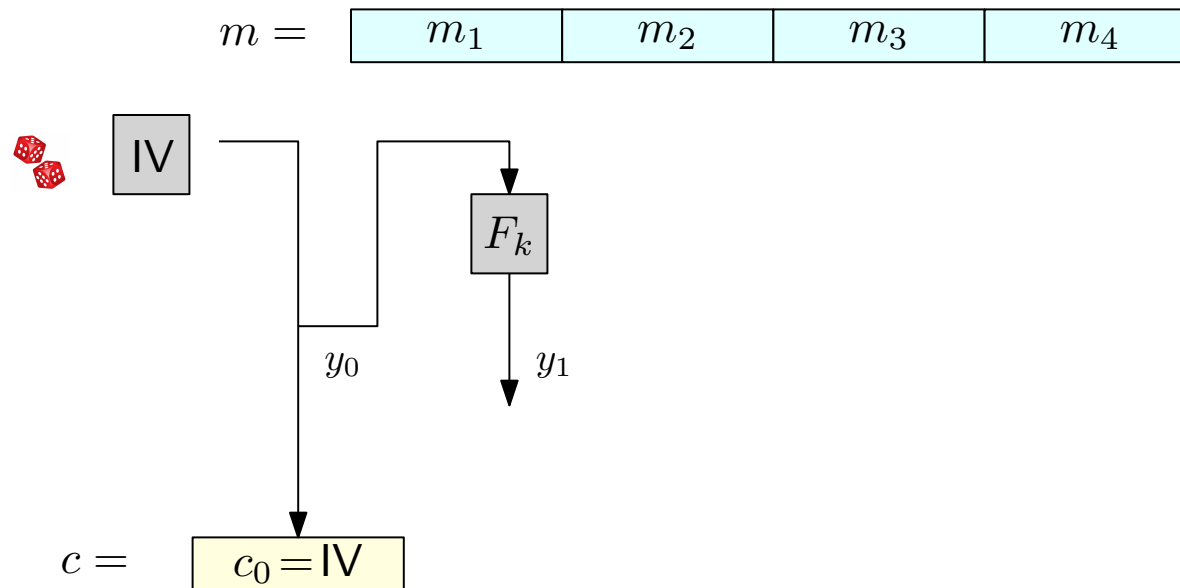
m_1	m_2	m_3	m_4
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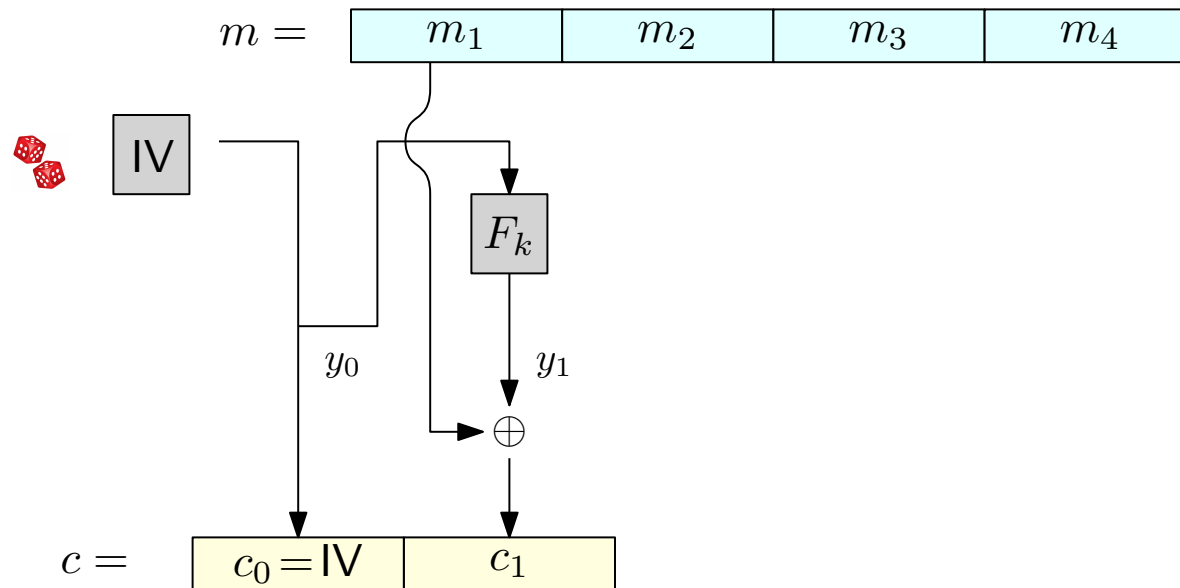
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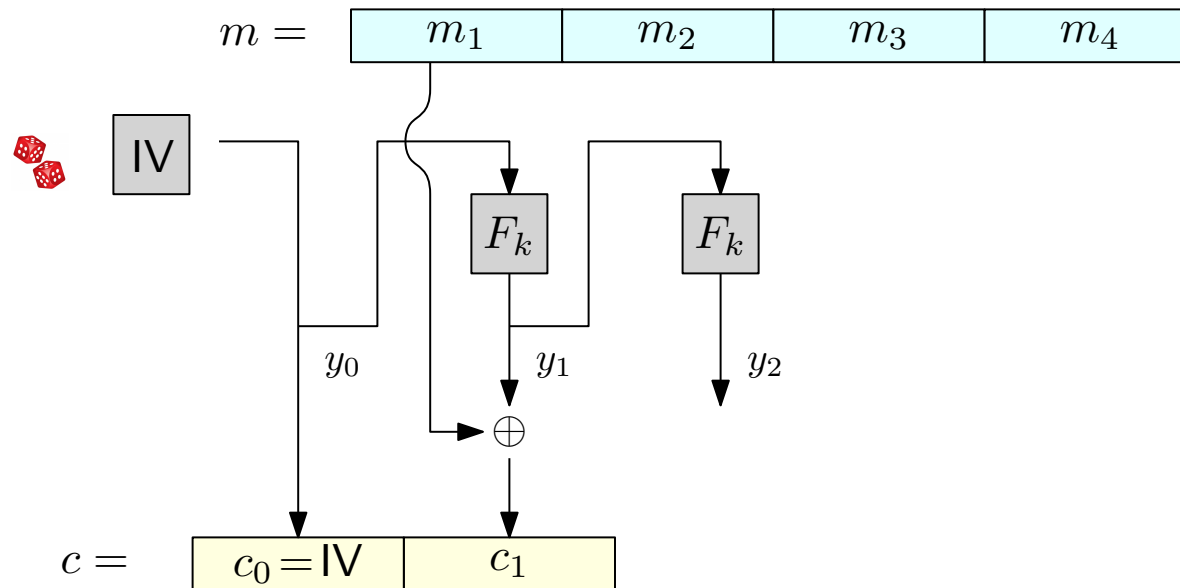
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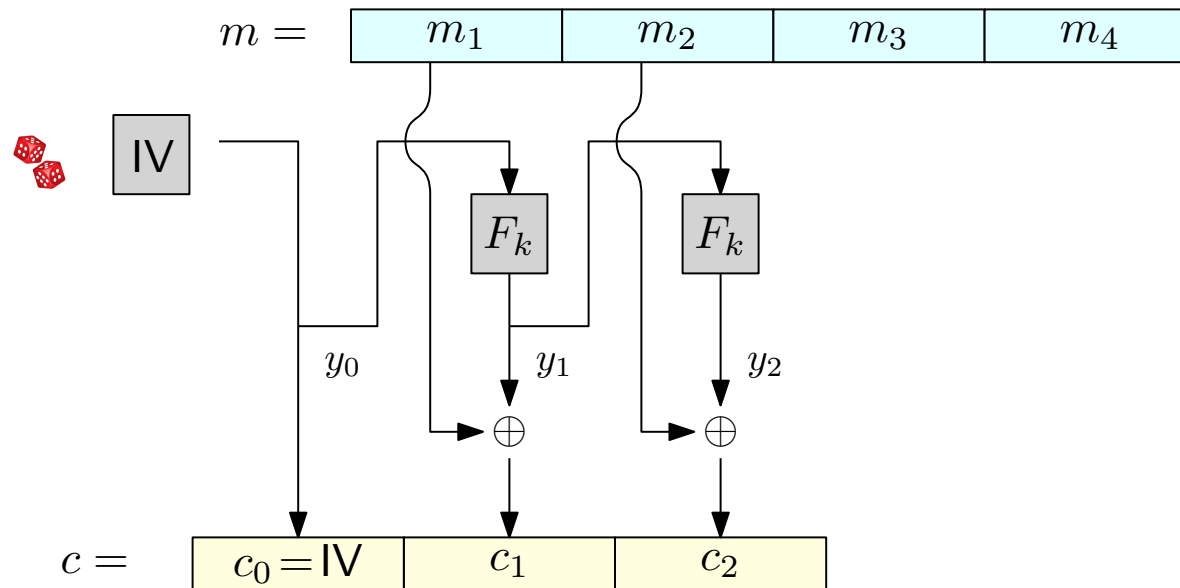
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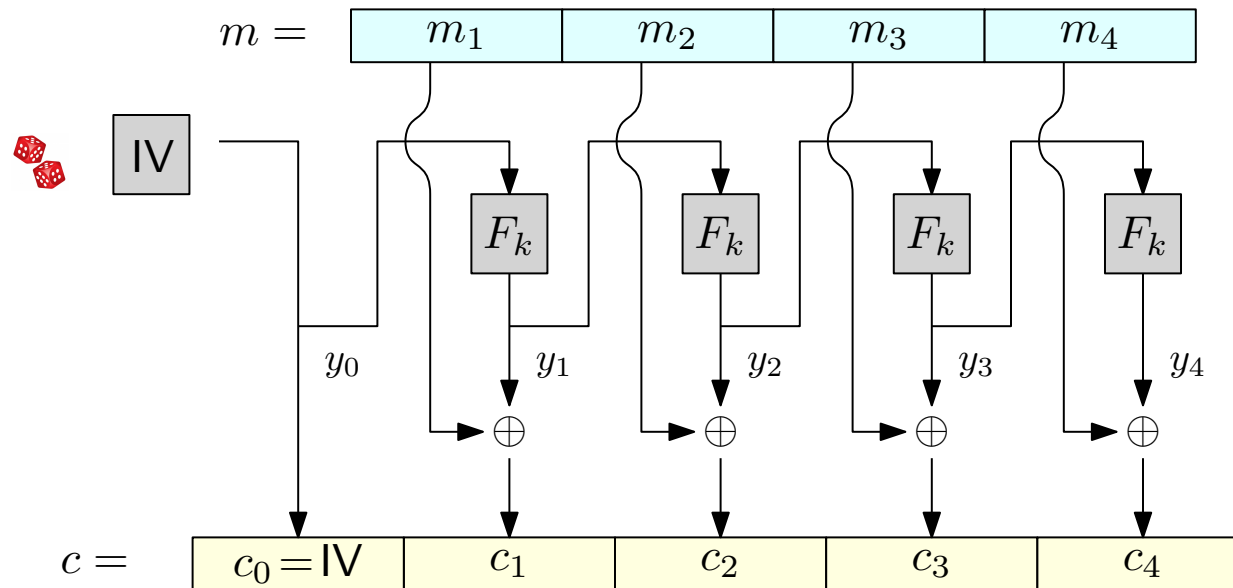
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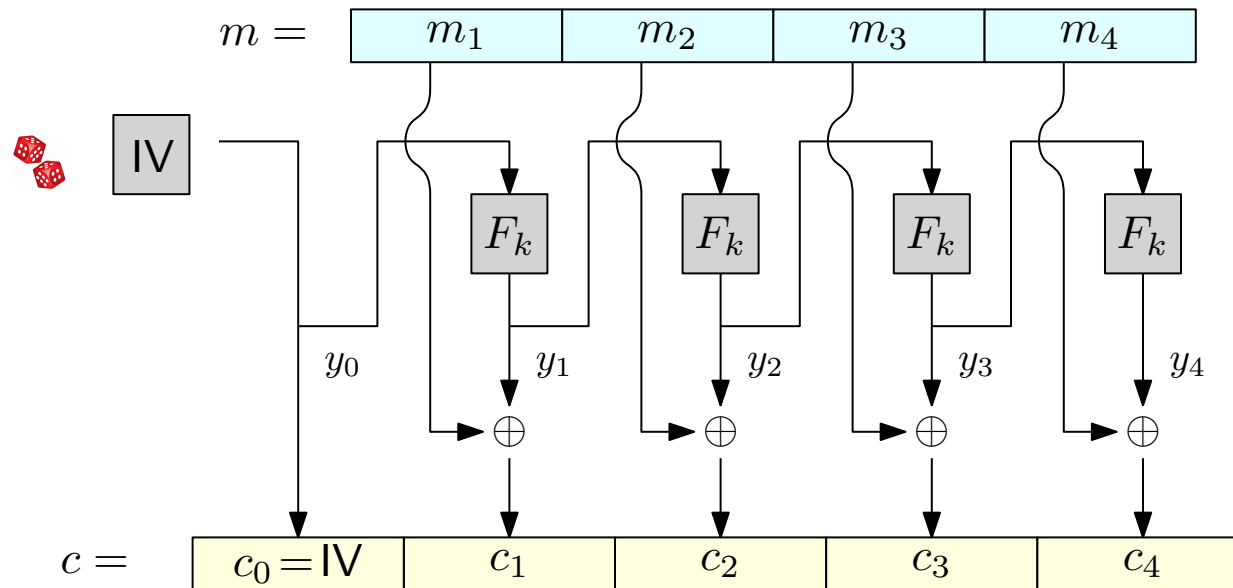
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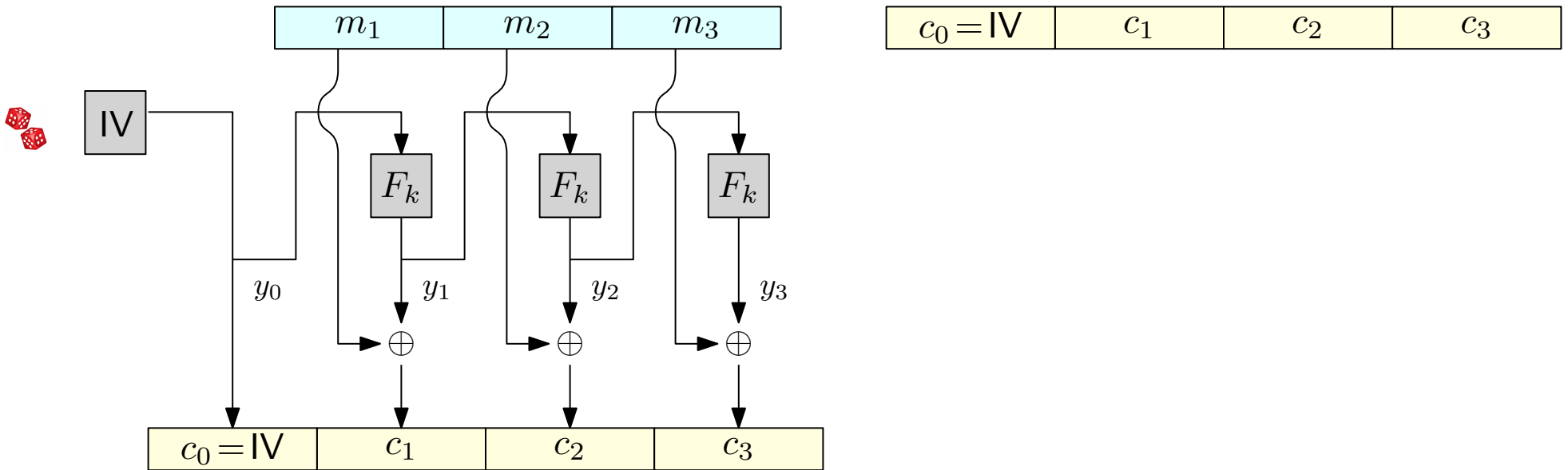


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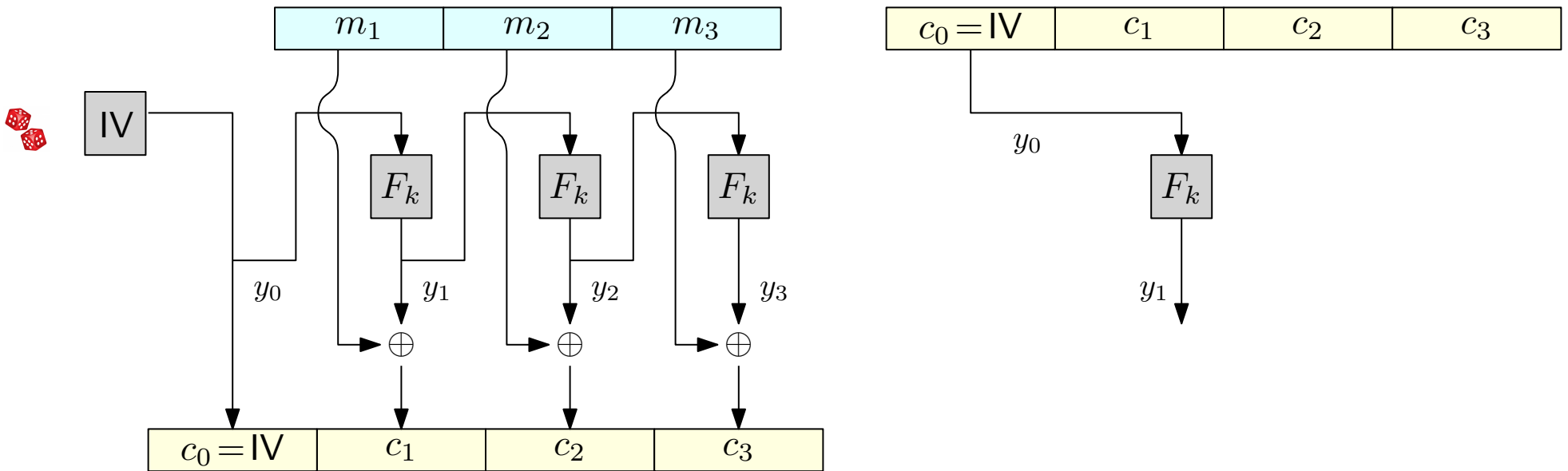
Can be thought of as a stream cipher (generate y_1, y_2, \dots and XOR it with the message)

Output Feedback (OFB) mode



Decrypting:

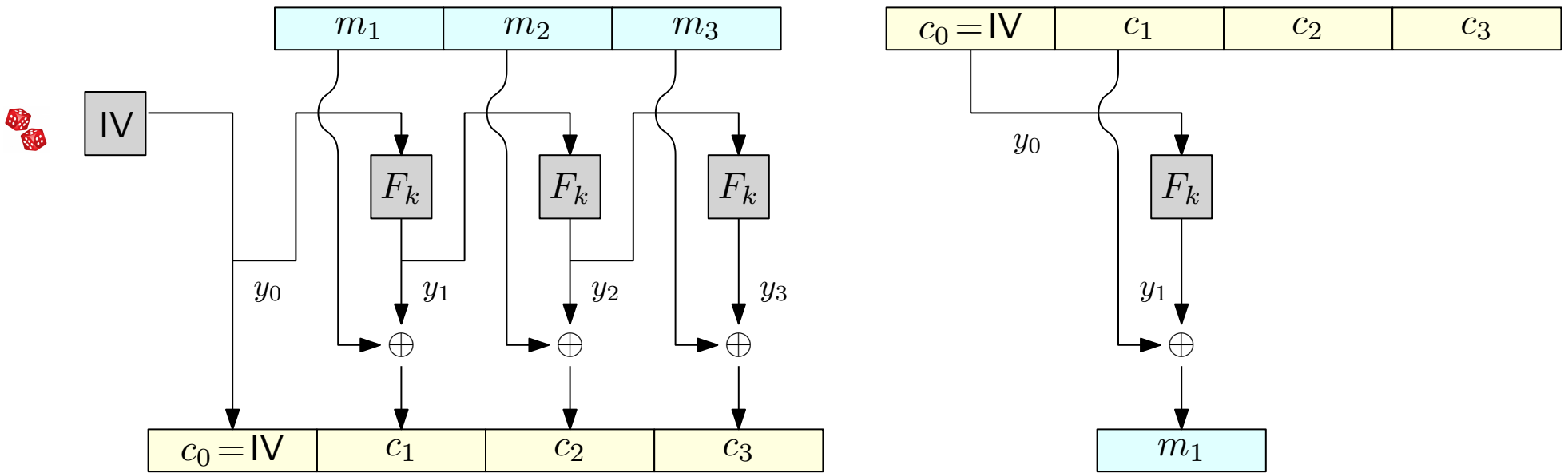
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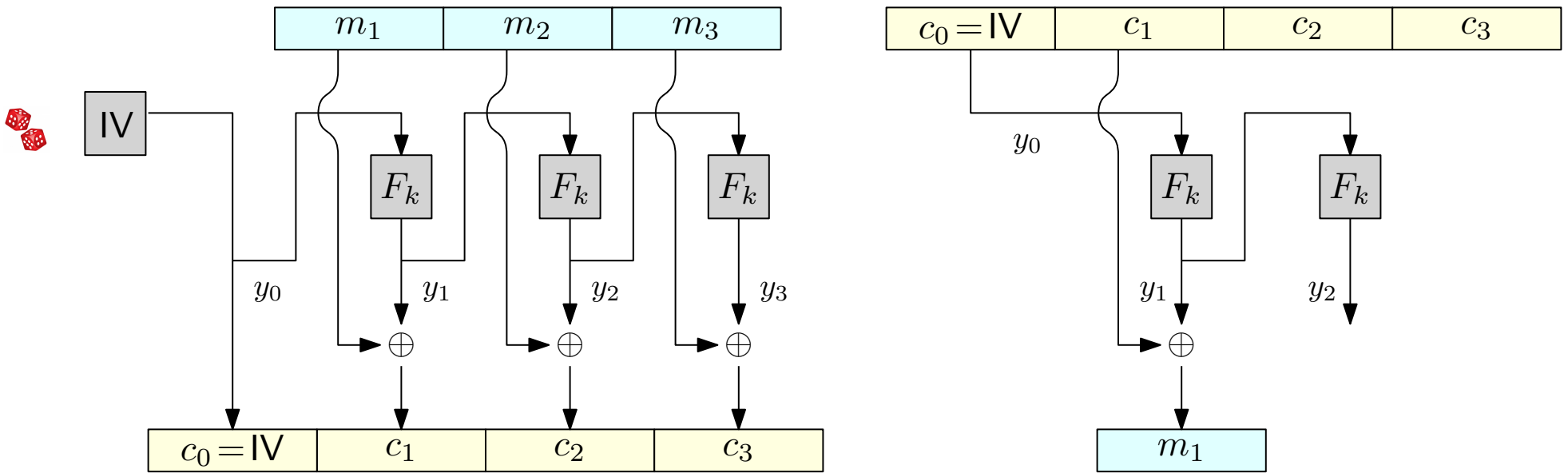
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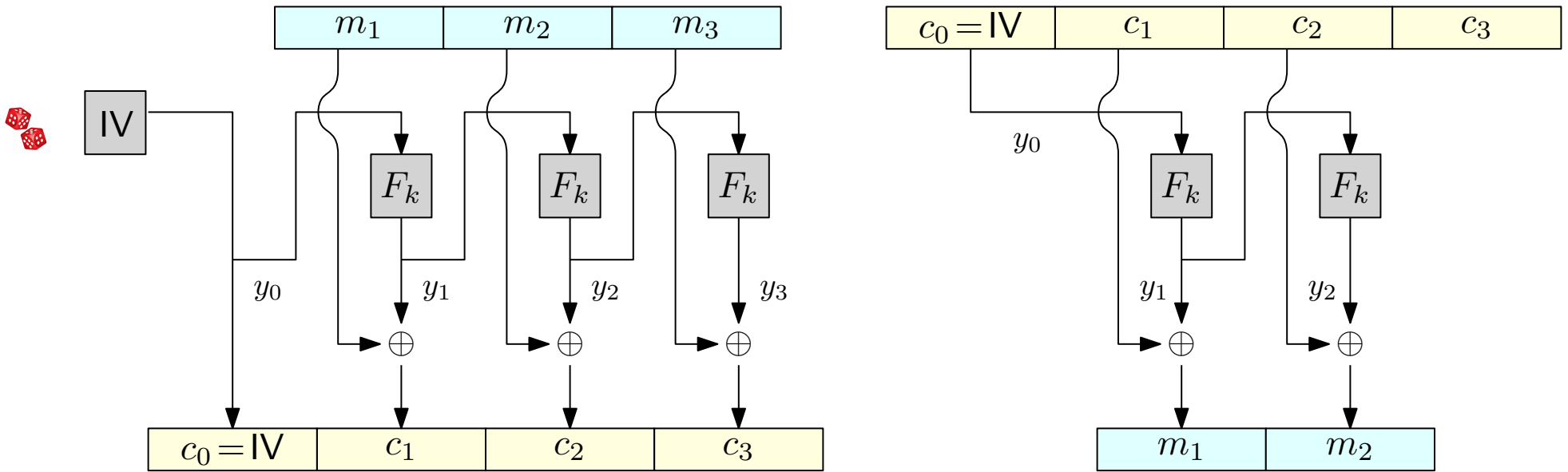
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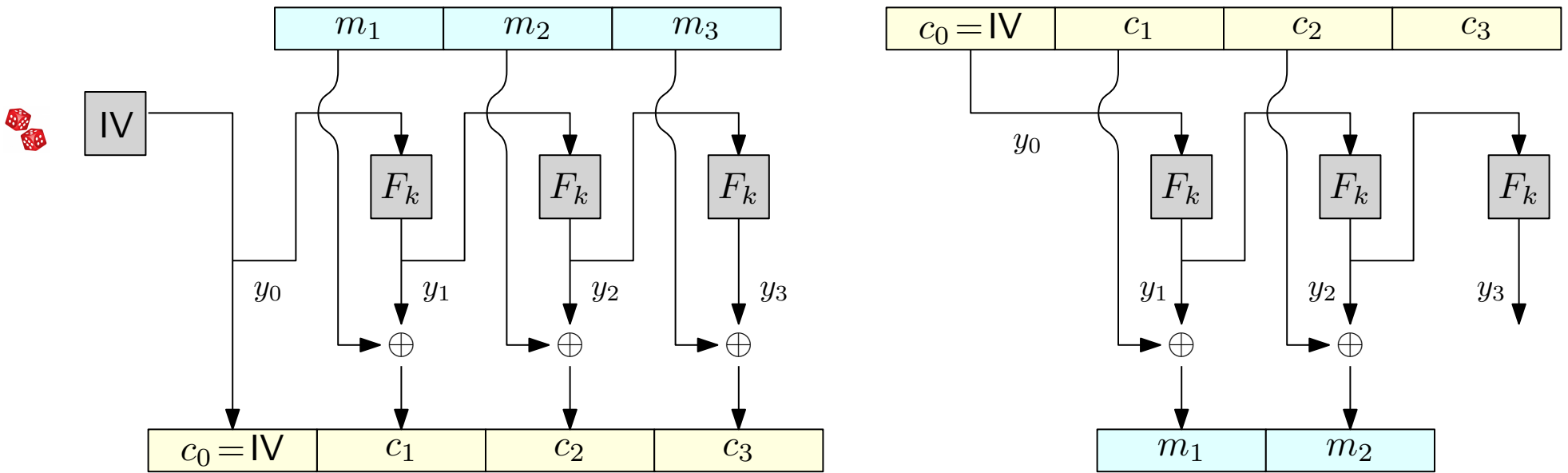
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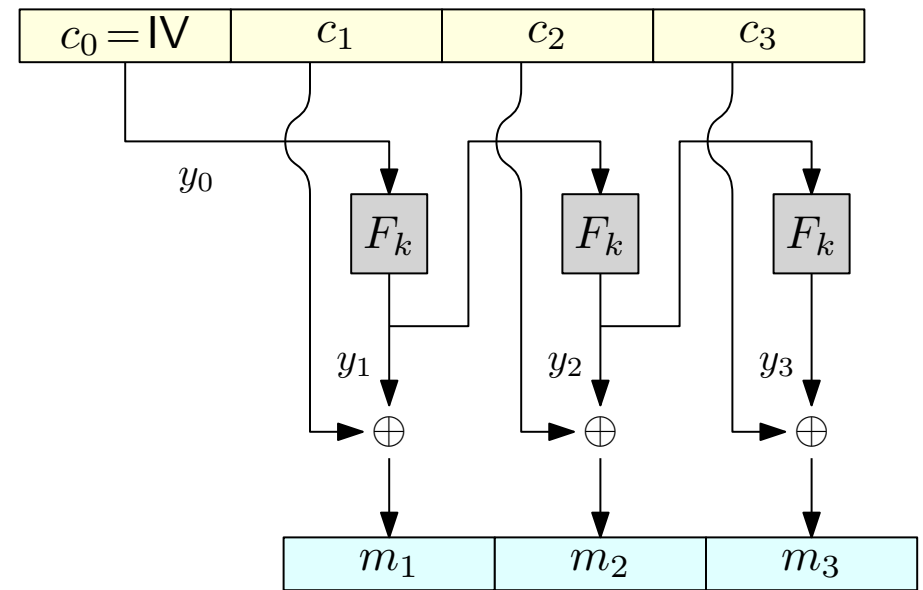
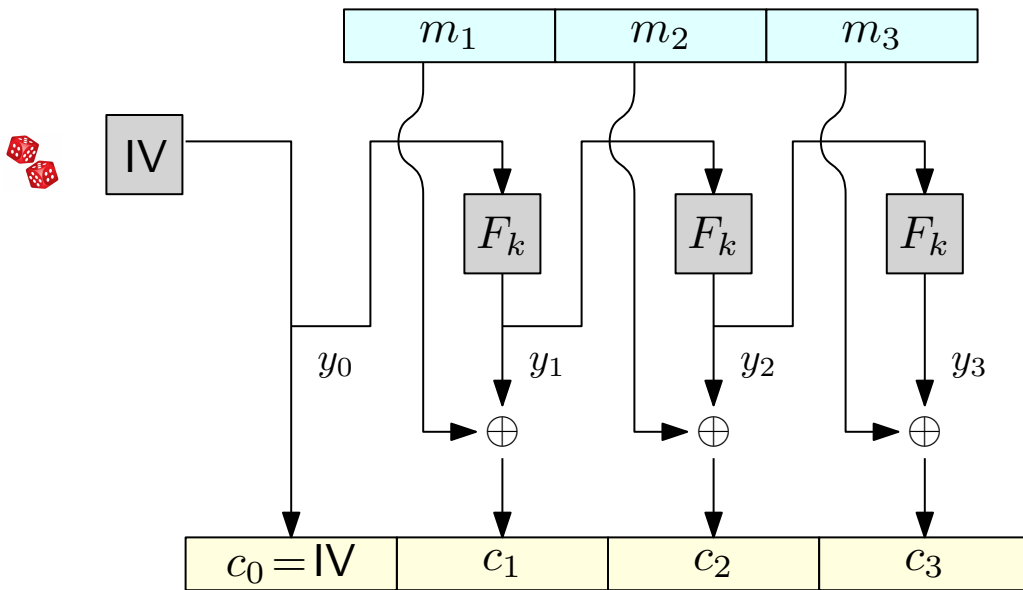
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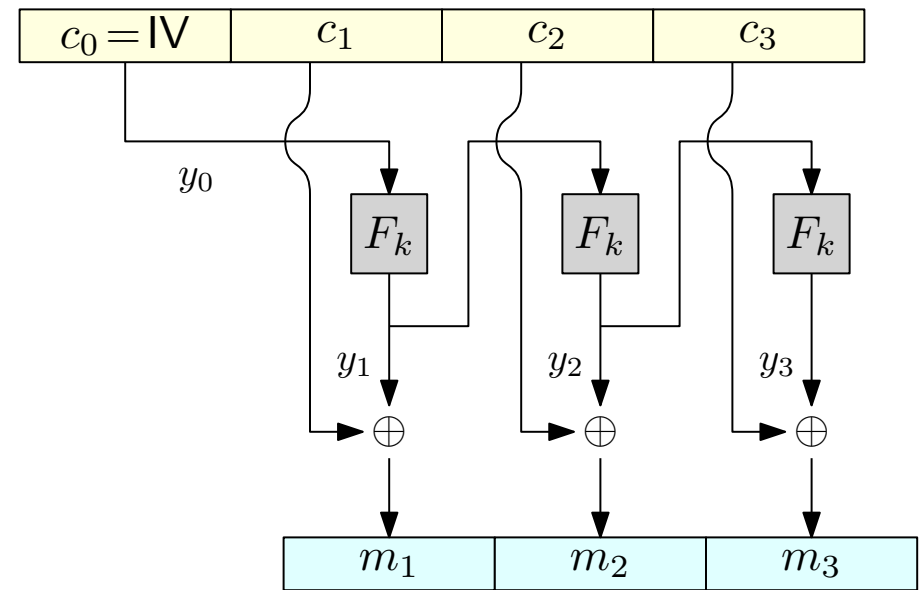
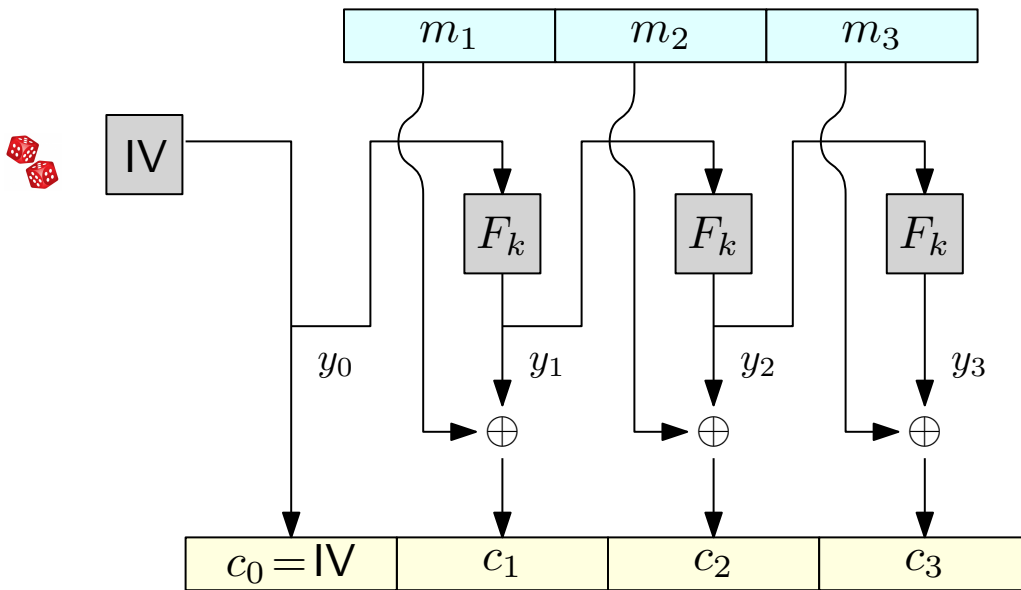
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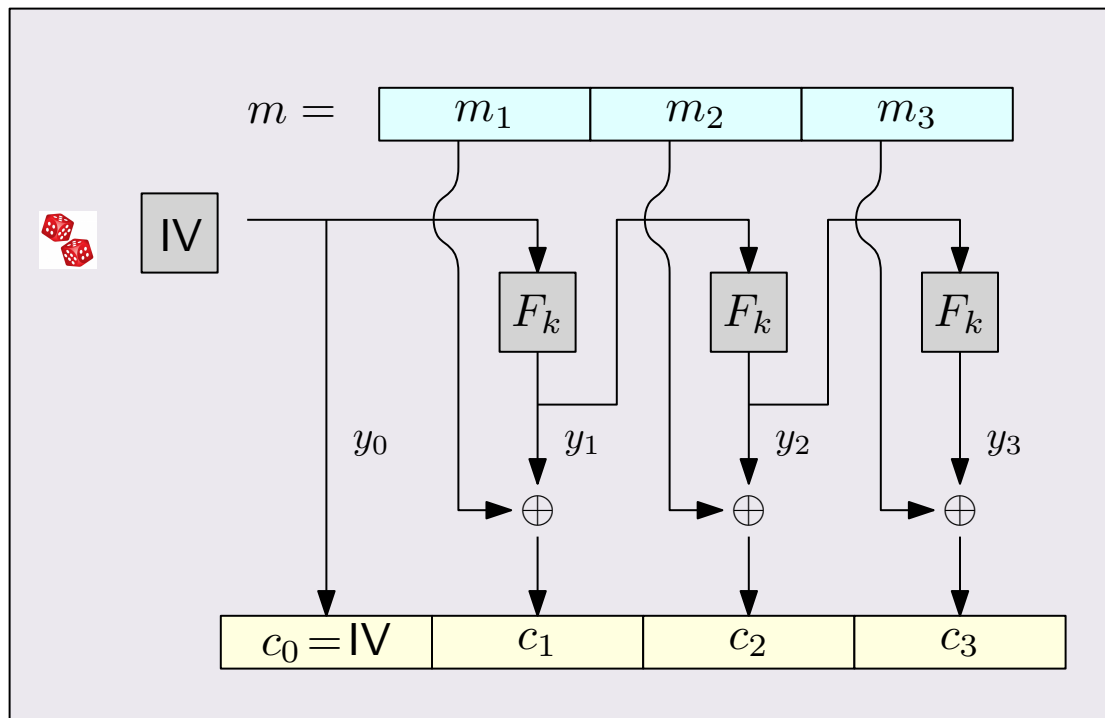
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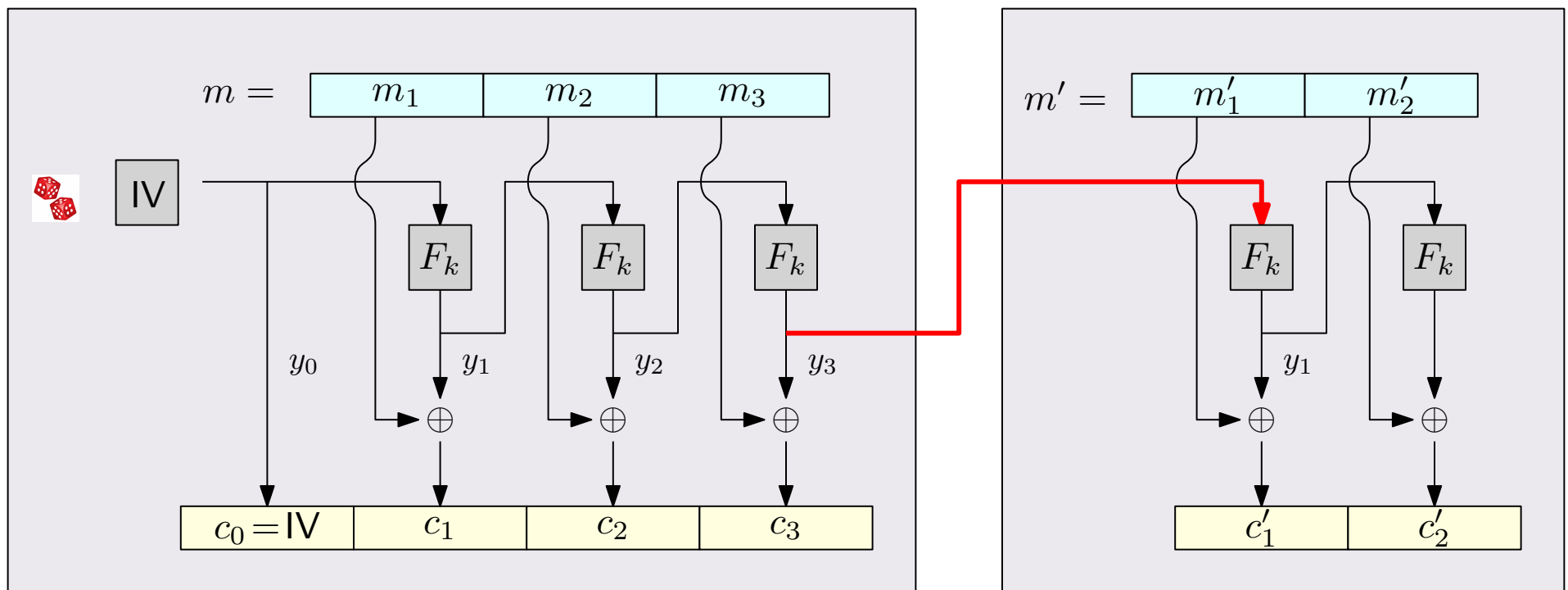
Output Feedback (OFB) mode, stateful variant

The stateful variant of OFB (the final value y_i is used in place of y_0 when the next message needs to be encrypted) is also **CPA-secure**



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Counter (CTR) mode

Can be viewed as a stream cipher

- Split the input to F into an IV and a counter

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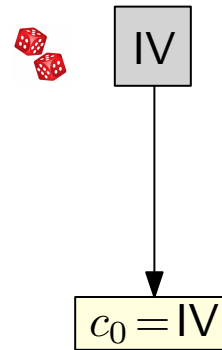
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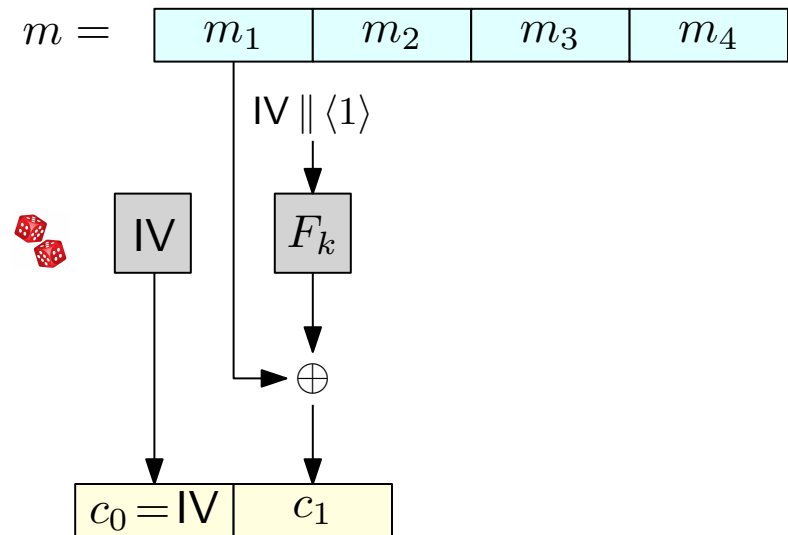
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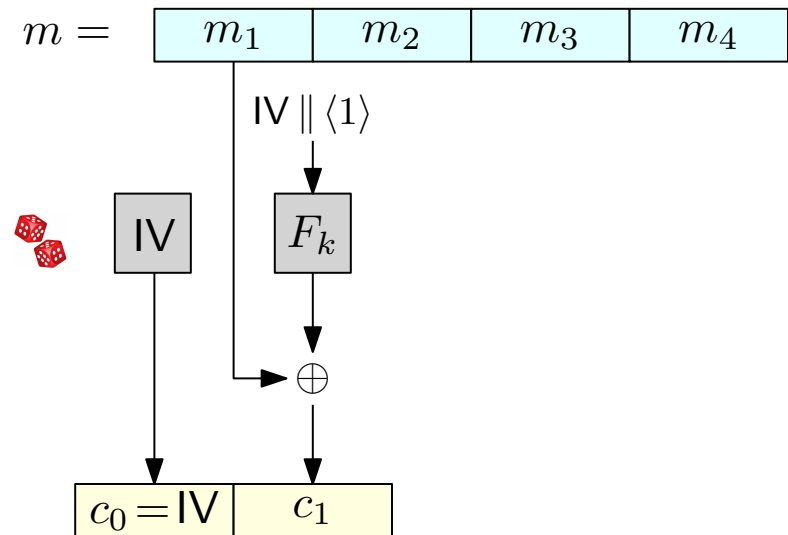
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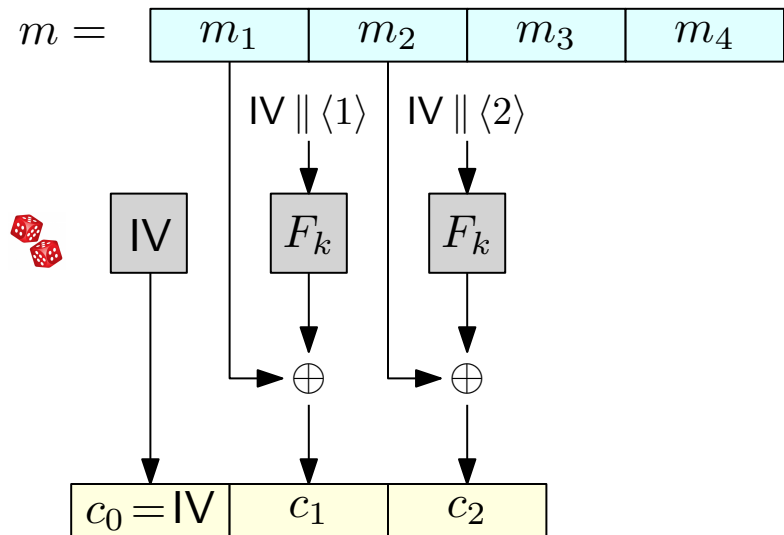
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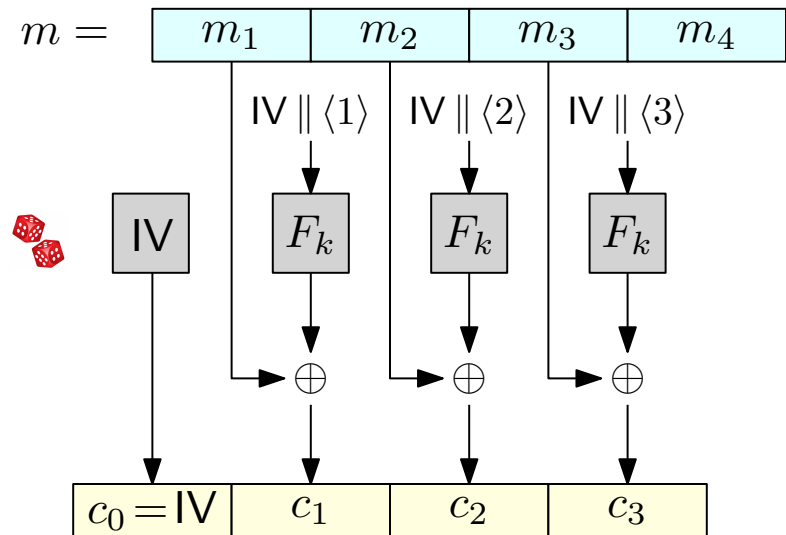
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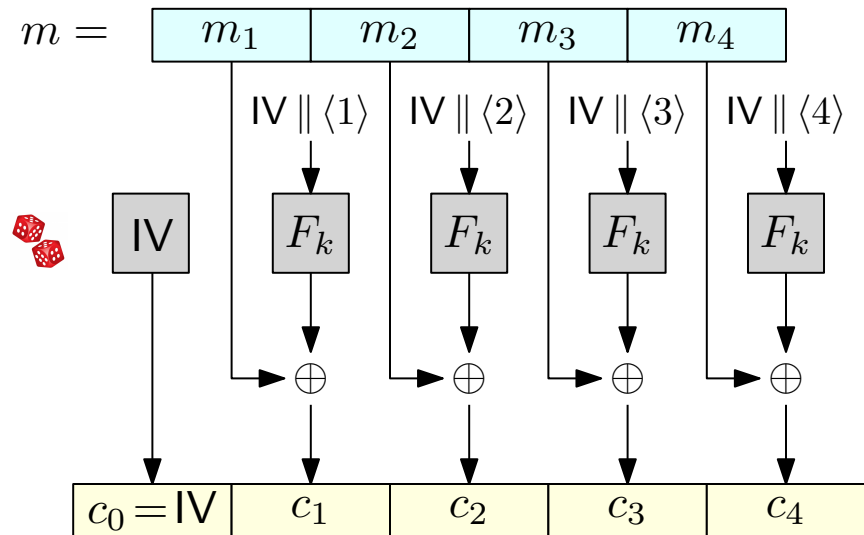
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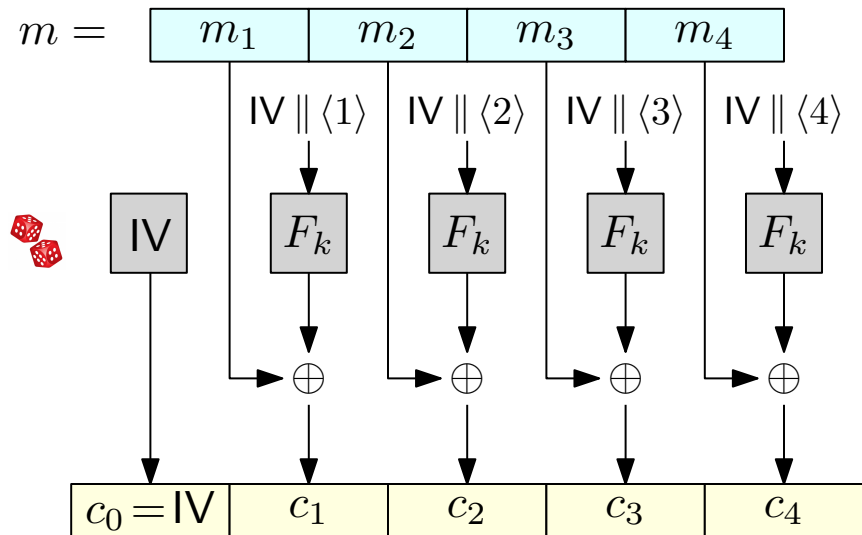
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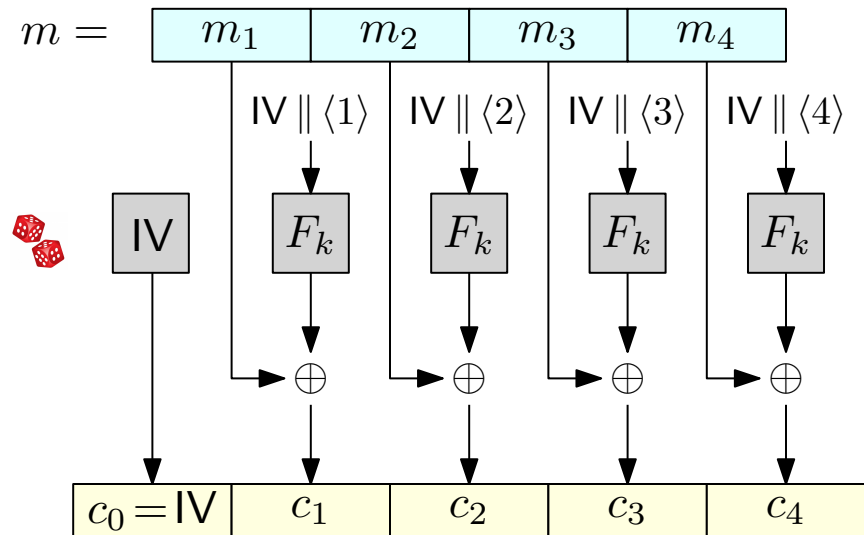
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- Remains secure even if IVs are not chosen u.a.r., in fact it suffices that IVs never repeat
$$\text{IV} = 00 \dots 000, 00 \dots 001, 00 \dots 010, 00 \dots 011, \dots$$